



CCGPS Frameworks Student Edition

Mathematics

Third Grade Unit Five
Geometry



Dr. John D. Barge, State School Superintendent
"Making Education Work for All Georgians"

Unit 5: GEOMETRY

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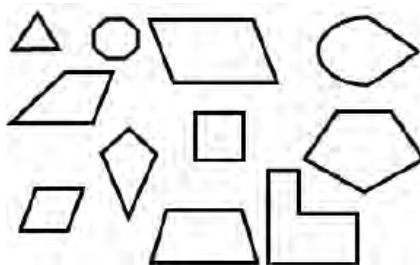
OVERVIEW

In this unit students will:

- Further develop understandings of geometric figures by focusing on identification and descriptions of plane figures based on geometric properties.
- Identifies examples and non-examples of plane figures and solid figures based on geometric properties.
- Identify differences among quadrilaterals.
- Understand that shapes in different categories may share attributes and those attributes can define a larger category (example: rhombuses, rectangles, and others have four sides and are all called quadrilaterals).
- Expand the ability to see geometry in the real world.
- Can draw plane figure shapes based on attributes.
- Further develop understanding of partitioning shapes into parts with equal areas.
- Partitions shapes in several different ways into equal parts of halves, thirds, fourths, sixths, and eighths and recognizes the partitioned parts have the same area.
- Use data collected to make bar and picture graphs.
- Interpret line plots.

Third Grade students will describe, analyze, and compare properties of two-dimensional shapes. They compare and classify shapes by their sides and angles, and connect these with definitions of shapes. Students also relate their fraction work to geometry by expressing the area of part of a shape as a unit fraction of the whole. Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language.

In second grade, students identify and draw triangles, quadrilaterals, pentagons, and hexagons. Third graders build on this experience and further investigate quadrilaterals (technology may be used during this exploration). Students recognize shapes that are and are not quadrilaterals by examining the properties of the geometric figures. They conceptualize that a quadrilateral must be a closed figure with four straight sides and begin to notice characteristics of the angles and the relationship between opposite sides. Students should be encouraged to provide details and use proper vocabulary when describing the properties of quadrilaterals. They sort geometric figures (see examples below) and identify squares, rectangles, and rhombuses as quadrilaterals.



Students should classify shapes by attributes and by drawing shapes that fit specific categories. For example, parallelograms include: squares, rectangles, rhombi, or other shapes that have two pairs of parallel sides. Also, the broad category, quadrilaterals, includes all types of parallelograms, trapezoids and other four-sided figures.

Students should also use this standard to help build on their understanding of fractions and area. Students are responsible for partitioning shapes into halves, thirds, fourths, sixths and eighths. Given a shape, students partition it into equal parts, recognizing that these parts all have the same area. They identify the fractional name of each part and are able to partition a shape into parts with equal areas in several different ways.

As an ongoing process throughout all third grade units, students should continue to develop understanding of representing and interpreting data using picture and bar graphs. They should also continue their work in generating measurement data by measuring lengths with rulers marked with halves and fourths of an inch. In second grade, students measured length in whole units using both metric and U.S. customary systems. It is important to review with students how to read and use a standard ruler including details about half and quarter marks on the ruler. Students should connect their understanding of fractions to measuring to one-half and one-quarter inch. Third graders need many opportunities measuring the length of various objects in their environment. This standard provides a context for students to work with fractions by measuring objects to a quarter of an inch.

With geometry, many student misconceptions might occur. The four content goals for geometry include shapes and properties, transformation, location, and visualization (see Van de Walle, page 205.) Students often have a difficult time recognizing shapes if the shape has been transformed by a translation, reflection, or rotation. Students may also identify a square as a “non-rectangle” or a “non-rhombus” based on limited images they see. They do not recognize that a square is a rectangle because it has all of the properties of a rectangle. They may list properties of each shape separately, but not see the interrelationships between the shapes. For example, students do not look at the properties of a square that are characteristic of other figures as well. Using straws to make four congruent figures have students change the angles to see the relationships between a rhombus and a square. As students develop definitions for these shapes, relationships between the properties will be understood.

<http://www.learner.org/courses/learningmath/geometry/session10/index35.html> - Lesson for the teacher to learn more about teaching Geometry to elementary students. The lesson includes ideas for lessons, video of classrooms, etc.

STANDARDS FOR MATHEMATICAL CONTENT

Mathematical standards are interwoven and should be addressed throughout the year in as many different units and activities as possible in order to emphasize the natural connections that exist among mathematical topics.

Reason with shapes and their attributes.

MCC3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

MCC3.G.2 Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.*

Represent and Interpret Data

MCC3.MD.3 Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs. *For example, draw a bar graph in which each square in the bar graph might represent 5 pets.*

MCC3.MD.4. Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units— whole numbers, halves, or quarters.

STANDARDS FOR MATHEMATICAL PRACTICE

Students are expected to:

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

*****Mathematical Practices 1 and 6 should be evident in EVERY lesson*****

ENDURING UNDERSTANDINGS

- Identify and describe properties of two-dimensional shapes using properties that are shared between the shapes.
- Generalize that shapes fit into a particular classification.
- Compare and classify shapes by their sides and angles, and connect these with definitions of shapes.
- Geometric figures can be classified according to their properties.
- Quadrilaterals can be classified according to the lengths of their sides.
- Recognize shapes that are and are not quadrilaterals by examining the properties of the geometric figures.
- Conceptualize that a quadrilateral must be a closed figure with four straight sides and begin to notice characteristics of the angles and the relationship between opposite sides
- Provided details and use proper vocabulary when describing the properties of quadrilaterals.
- Sort geometric figures and identify squares, rectangles, and rhombuses as quadrilaterals.
- Classify shapes by attributes and by drawing shapes that fit specific categories. (e.g.; parallelograms include: squares, rectangles, rhombi, or other shapes that have two pairs of parallel sides.
- The broad category “Quadrilaterals” includes all types of parallelograms, trapezoids and other four-sided figures.

- Relate fraction work to geometry by expressing the area of a shape as a unit fraction of the whole.
- Shapes can be partitioned with equal areas in a variety of ways to show halves, thirds, fourths, sixths, and eighths.

ESSENTIAL QUESTIONS

- Can a shape be represented in more than one way? How and why?
- How are quadrilaterals alike and different?
- How are solid figures different from plane figures?
- How can angle and side measures help us to create and classify quadrilaterals?
- How can I use attributes to compare and contrast shapes?
- How can partitioning a shape into halves, thirds, fourths, sixths, or eighths in a variety of ways help me further develop my understanding of fractions?
- How can plane figures be combined to create new figures?
- How can shapes be combined to create new shapes?
- How can solid figures be categorized and classified?
- How can we communicate our thinking about mathematical vocabulary?
- How can you create different types of quadrilaterals?
- How does combining figures affect the attributes of those figures?
- What are the properties of quadrilaterals?
- What is a quadrilateral?
- What properties do solid figures have in common?
- Why are units important in measurement?
- Why is it important to partition shapes into equal areas?

CONCEPTS/SKILLS TO MAINTAIN

It is expected that students will have prior knowledge/experience related to the concepts and skills identified below. It may be necessary to pre-assess in order to determine if time needs to be spent on conceptual activities that help students develop a deeper understanding of these ideas.

- Represent and solve problems involving multiplication and division
- Understand properties of multiplication and the relationship between multiplication and division
- Multiply and divide within 100
- Solve problems involving the four operations, and identify and explain patterns in arithmetic
- Use place value
- Recognize basic geometric figures and spatial relationships of triangle, quadrilateral (squares, rectangles, and trapezoids), pentagon, hexagon, cube, trapezoid, half/quarter circle, circle, cone, cylinder, sphere

SELECTED TERMS AND SYMBOLS

The following terms are often misunderstood. These concepts are not an inclusive list and should not be taught in isolation. However, due to evidence of frequent difficulty and misunderstanding associated with these concepts, instructors should pay particular attention to them and how their

students are able to explain and apply them. These terms are **for teacher reference only** and are not to be memorized by the students. Teachers should present these concepts to students with models and real life examples. Students should understand the concepts involved and be able to recognize and/or demonstrate them with words, models, pictures, or numbers.

- 2-dimensional
- 3-dimensional
- acute angle
- attributes
- closed figure
- congruent
- cubes, cones, cylinders and rectangular prisms (as subcategories of 3-dimensional figures)
- polygon
- line plot
- obtuse angle
- open figure
- parallel
- parallelogram
- partition
- polygon
- properties
- quadrilateral
- rectangle
- rhombi, rectangles, and squares (as subcategories of quadrilaterals)
- rhombus/rhombi
- right angle
- square
- three-sided
- unit fraction

Additional resources for finding definitions for common geometry terms:

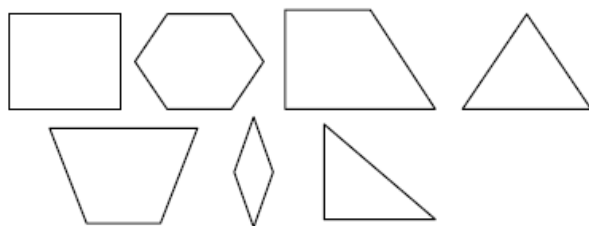
<http://www.amathsdictionaryforkids.com/dictionary.html>
<http://www.mathleague.com/help/geometry/polygons.htm>

STRATEGIES FOR TEACHING AND LEARNING:

In earlier grades, students have experiences with informal reasoning about particular shapes through sorting and classifying using their geometric attributes. Students have built and drawn shapes given the number of faces, number of angles and number of sides.

The focus now is on identifying and describing properties of two-dimensional shapes in more precise ways using properties that are shared rather than the appearances of individual shapes. These properties allow for generalizations of all shapes that fit a particular classification. Development in focusing on the identification and description of shapes' properties should include examples and non-examples, as well as examples and non-examples drawn by students of shapes in

a particular category. For example, students could start with identifying shapes with right angles. An explanation as to why the remaining shapes do not fit this category should be discussed. Students should determine common characteristics of the remaining shapes.



In Grade 2, students partitioned rectangles into two, three or four equal shares, recognizing that the equal shares need not have the same shape. They described the shares using words such as, halves, thirds, half of, a third of, etc., and described the whole as two halves, three thirds or four fourths. In Grade 3 students will partition shapes into parts with equal areas (the spaces in the whole of the shape). These equal areas need to be expressed as unit fractions of the whole shape, i.e., describe each part of a shape partitioned into four parts as $\frac{1}{4}$ of the area of the shape.

Have students draw different shapes and see how many ways they can partition the shapes into parts with equal areas.

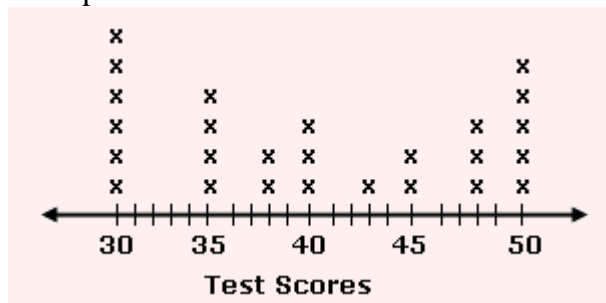
<http://www.learner.org/courses/learningmath/geometry/pdfs/session9/vand.pdf> - Geometric Thinking from John Van de Walle

<http://print.nycenet.edu/NR/ronlyres/0EFD73D4-340A-42E2-8EB4-3BC2A6B05603/38319/30vanHielePlay.pdf> - Developing Geometric Thinking Through Activities that Begin With Play – By Pierre van Hiele

Also in the unit, students will use what they have learned in second grade about representing the length of several objects by making a line plot. In second grade, students would have rounded their lengths to the nearest whole unit. A line plot shows data on a number line with an **X** or other mark to show frequency.

Examples of Line Plot

- The line plot below shows the test scores of 26 students.



The count of cross marks above each score represents the number of students who obtained the respective score. For students in second and third grade, they will use the data from measuring with rulers to create line plots.

EVIDENCE OF LEARNING

By the conclusion of this unit, students should be able to demonstrate the following competencies:

- Identify and draw triangles, quadrilaterals (square, rectangle, parallelogram, trapezoid, and rhombus), pentagons, and hexagons.
- Draw common polygons.
- Sort, compare and classify geometric figures according to their properties.
- Identify and describe examples and non-examples of shapes based on properties.
- Partition shapes into equal shares of halves, thirds, fourths, sixths, and eighths.
- Use tangrams to combine (compose) shapes to make other shapes.
- Reason with shapes and their attributes.
- Create a bar graph and picture graph with a scale of 2, 5, or 10 based on a geometric picture
- Use a ruler to measure the sides of several shapes and create a line plot with the data.

TASKS

Scaffolding Task	Constructing Task	Practice Task	Performance Tasks
Tasks that build up to the constructing task.	Constructing understanding through deep/rich contextualized problem solving tasks	Games/activities	Summative assessment for the unit.

<u>Task Name</u>	Type of Task/ Grouping Strategy	Skills
Show What You Know	Scaffolding/ Individual	Describing, Drawing Shapes
Shape Sorter	Scaffolding/ Group/Partner	Comparing/Contrasting, Classifying Shapes
What Makes A Shape?	Constructing/ Group/Partner	Sorting and Classifying Shapes
Properties of Quadrilaterals	Constructing/ Group/Partner	Defining Quadrilaterals
Can You Find It?	Practice/ Individual/Partner	Identifying Shape
Score It!	Practice/ Individual/Partner	Identifying Shapes Within Other Shape
Geoboard Geometry Guru	Constructing/ Group/Individual	Defining Shapes
Tangram Challenge	Constructing/ Group/Individual	Combining & Creating Geometric Figures

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How Much Are My Tangrams Worth?	Practice/ <i>Individual/Partner</i>	Combining & Creating Geometric Figures
How Many Different Ways?	Practice/ <i>Individual/Partner</i>	Combining Shapes to Fill an Area
Tangram Puzzle	Practice/ <i>Individual/Partner</i>	Using Shapes to Create a Larger Shape
Quadrilateral Challenge	Constructing/ <i>Individual/Partner/Group</i>	Defining Quadrilaterals
Quadrilateral Riddles	Practice/ <i>Individual/Partner</i>	Defining Quadrilaterals
What Do You See?	Practice/ <i>Individual</i>	Comparing/Contrasting Shapes
What's the Connection?	Constructing/ <i>Groups of 4</i>	Comparing Quadrilaterals
Pattern Block Fractions	Constructing/ <i>Partner</i>	Partitioning Shapes
Picture Pie	Practice/ <i>Individual/ Partner</i>	Using Shapes to Create Art
Pattern Block Graphing	Constructing/ <i>Individual/ Partner</i>	Constructing Shapes to Create Pictures; Collect Data and Create Graphs
I Has, Who Has?	Practice/ <i>Group</i>	Using Pictorial Representation of Fractions
Measure My Shapes	Constructing/ <i>Individual/Partner</i>	Measuring Sides to Create Line Plots
My Geometric Booklet	Constructing/ <i>Individual/ Partner/Group</i>	Reasoning with shapes, Partitioning Shapes
Choice Board	Culminating Task	Reasoning with shapes, Partitioning shapes, Representing and interpreting data

SCAFFOLDING TASK: SHOW WHAT YOU KNOW!



STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.

BACKGROUND

Students should have had experience with identifying two-dimensional shapes (no matter the position, orientation, or size) and begin to use the properties of the shapes to further develop understanding of shapes. These properties can include number of sides, number of corners (vertices), and may have included the length of the sides. Two-dimensional shapes include triangles, quadrilaterals (square, rectangle, and trapezoids), circles, pentagons, and hexagons. In third grade, students will further develop their understanding of two-dimensional shapes by looking at the different categories and the attributes that shapes might share.

ESSENTIAL QUESTIONS

- Why do we study shapes?
- How do the attributes help us identify the different shapes?
- What are some different ways to identify shapes?
- What is the different between an attribute and a property of a shape?

MATERIALS

- Student Copy of “Show What You Know” Recording Sheet

GROUPING

Individual Activity

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

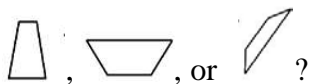
Teacher Directions: Students will use the recording sheet to show their current understanding of two-dimensional/plane shapes. This activity could be used as a formative assessment throughout this unit to show what students know at the beginning of the unit, during the unit, and at the end of the unit. If there is room to reuse the same sheet, have students changed the color of their writing utensil to show growth, or have students draw a line under the information after each assessment. This activity will also help you guide students in their development of their Geometric Thinking based on the van Hiele levels. More on the topic can be read in the Van de Walle 3-5 resource book on pages 206 - 208

FORMATIVE ASSESSMENT QUESTIONS

The Recording Sheet is a graphic organizer that can help you understand what students know about two-dimensional shapes. Other formative assessment questions might include:

- What are some differences between the shapes listed?
- Are any of the shapes alike?
- Can you give me an example of a (name a shape?) What about a non-example?
- Are all of these shapes the same?
- What if _____
_____?
_____?

Example: What if I added another side? What if this shape looked like



Is it still a trapezoid

DIFFERENTIATION

Extension

Students that need an extension with this activity might be able to use vocabulary to describe the sides and vertices of the different shapes. They might also be able to see that some of the shapes belong together in the same class and may be able to describe the properties of the shapes that belong in the same class.

Intervention

Students that struggle with this activity may not know different ways in which shapes can be described (attributes, properties) and only know a shape based on its appearance. Teachers may want to create an anchor chart with terms used in discussion so that students who struggle can refer to the anchor chart. Examples of these words might be: sides, corners/vertices, polygon, congruent, angle. Students should help produce the anchor chart.

TECHNOLOGY CONNECTIONS

- <http://www.harcourtschool.com/activity/buzz/buzz.html>

Name _____ Date _____

Plane Shapes

Use the space below to write, draw, or describe what you know about the shapes.

Rectangle

Square

Rhombus

Triangle

Trapezoid

Quadrilaterals

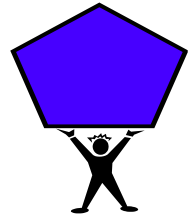
Pentagon

Hexagon

Circle

CONSTRUCTING TASK: SHAPE SORTER

Adapted from Activity 8.1 in Teaching Student Centered Mathematics 3-5, by John Van de Walle and LouAnn Lovin



STANDARDS FOR MATHEMATICAL CONTENT

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STANDARDS FOR MATHEMATICAL PRACTICES

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7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND

Students should have had experience with identifying two-dimensional shapes (no matter the position, orientation, or size) and begun to use the properties of the shapes to further develop understanding of shapes. These properties can include number of sides, number of corners (vertices), and may have included the length of the sides. Two-dimensional shapes include triangles, quadrilaterals (square, rectangle, and trapezoids), circles, pentagons, and hexagons.

ESSENTIAL QUESTIONS

- Is it possible for a square to be a rectangle? Is a rectangle a square?
- Do you think shapes might be grouped together in the same family or classification? Explain.
- How do you know the difference between shapes if several of them have the same number of sides?
- How is a rhombus different from a square, rectangle, or trapezoid?

MATERIALS

- An assortment of shapes for sorting
http://www.ablongman.com/vandewalleseries/Vol_2_BLM_PDFs/BLM20-26.pdf
 Or see the attached sheets
- Math Journals
- Chart Paper

GROUPING

Groups (4 students per group works well)/Individual

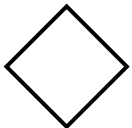

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

1. Divide students into groups of four. Each group of students should have an assortment of shapes. These shapes should be regular and irregular shapes. Once students are in groups, each student will pick a shape and tell 2 or 3 things they find interesting about the shape (No right or wrong answer.) You might want the students to write in their journal before sharing.
2. After all students share about their first shape, students will pick a second shape from the group's assortment. Each student will then try to find something that is the same about the two shapes and something that is different about the shapes chosen. Students may journal this before sharing with their group (see example of Compare/Contrast Matrix below). After comparing/contrasting the two shapes, students will share with their group. Students within the same group should begin to create a list of words that are common among the shapes. All words that describe the shapes should be accepted (pointed, curvy, lines look like train track, etc.) and then you can introduce the correct math vocabulary.

Example of Compare/Contrast Matrix

My Shapes are the	Attribute	Shape # 1	Shape #2
Same			
Different			

Student Example of Compare/Contrast Matrix

My Shapes are the:	Attribute	Shape # 1	Shape #2
			
Same	Has a corner like an L	Yes	No
Different	All sides are the same length	Yes	No

3. Allow all groups to share with the class the similarities and differences between the shapes. Make a class anchor chart of words that describe shapes. This anchor chart might include the words: sides, angles, corner/vertices, and the names of shapes.

4. The group will continue exploring the shapes by selecting one shape at random and placing it in the center of the group. The task for the group is to find all of the other shapes that are like the target shape (which is the shape that is in the center of the group) according to the same rule. Students might say, “This shape is like the target shape because it has _____ and _____.”

Example: This shape is like the target shape because it has curves and one straight side.

Challenge students to use the same target shape but sort the shapes using a different property. For students that struggle with this challenge, have them refer back to the anchor chart to pick another property.

FORMATIVE ASSESSMENT QUESTIONS






- Describe your shape to me.
- Why does this shape belong with these shapes and not in this other group?
- How might this shape fit with these?
- Did you learn any new words today? What does the word _____ mean? Draw a picture to show the word?
- Do you agree with your group members’ decisions about the categories chosen for each shape? Did you see the shape in a different way?

DIFFERENTIATION

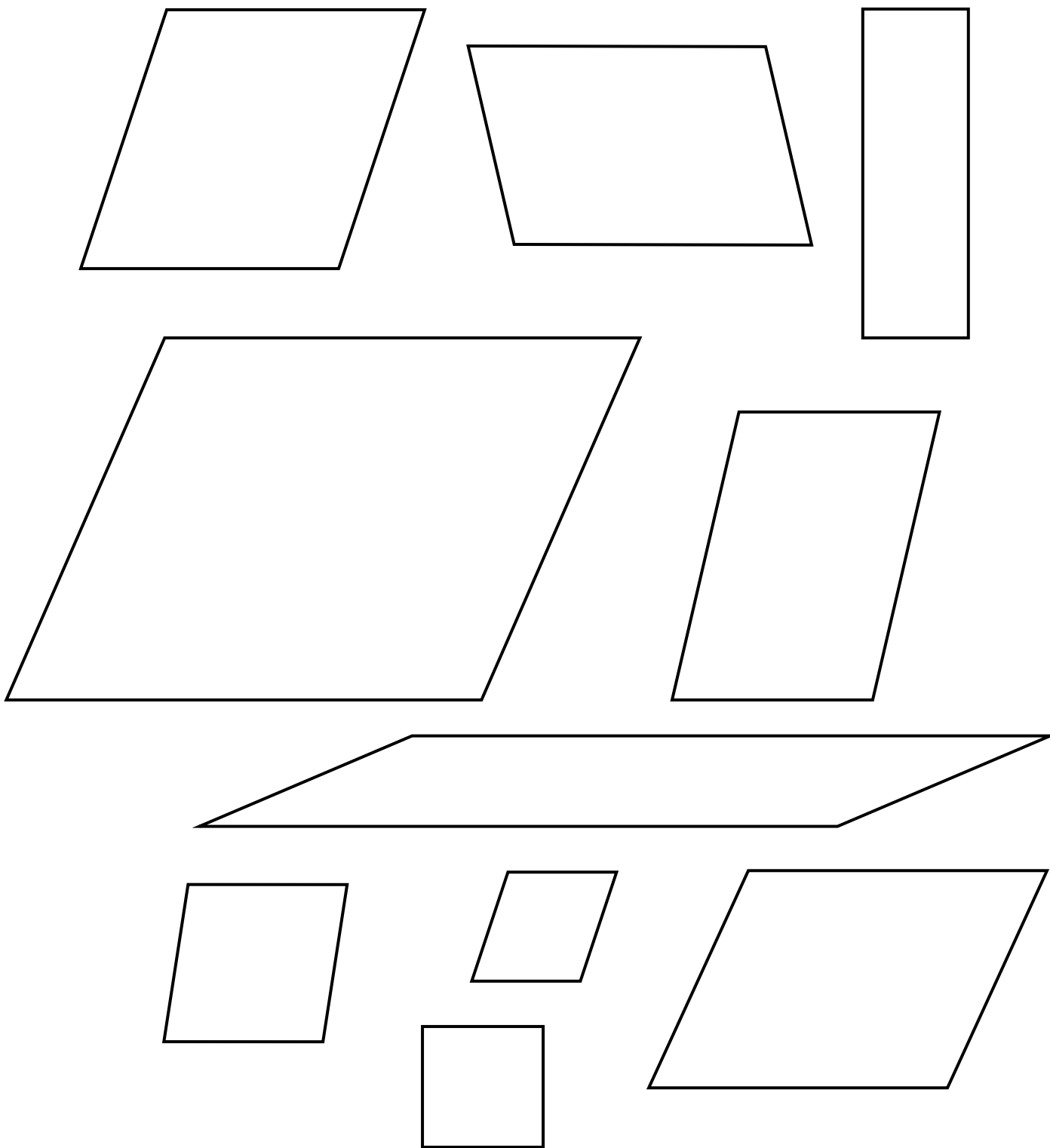
Extension

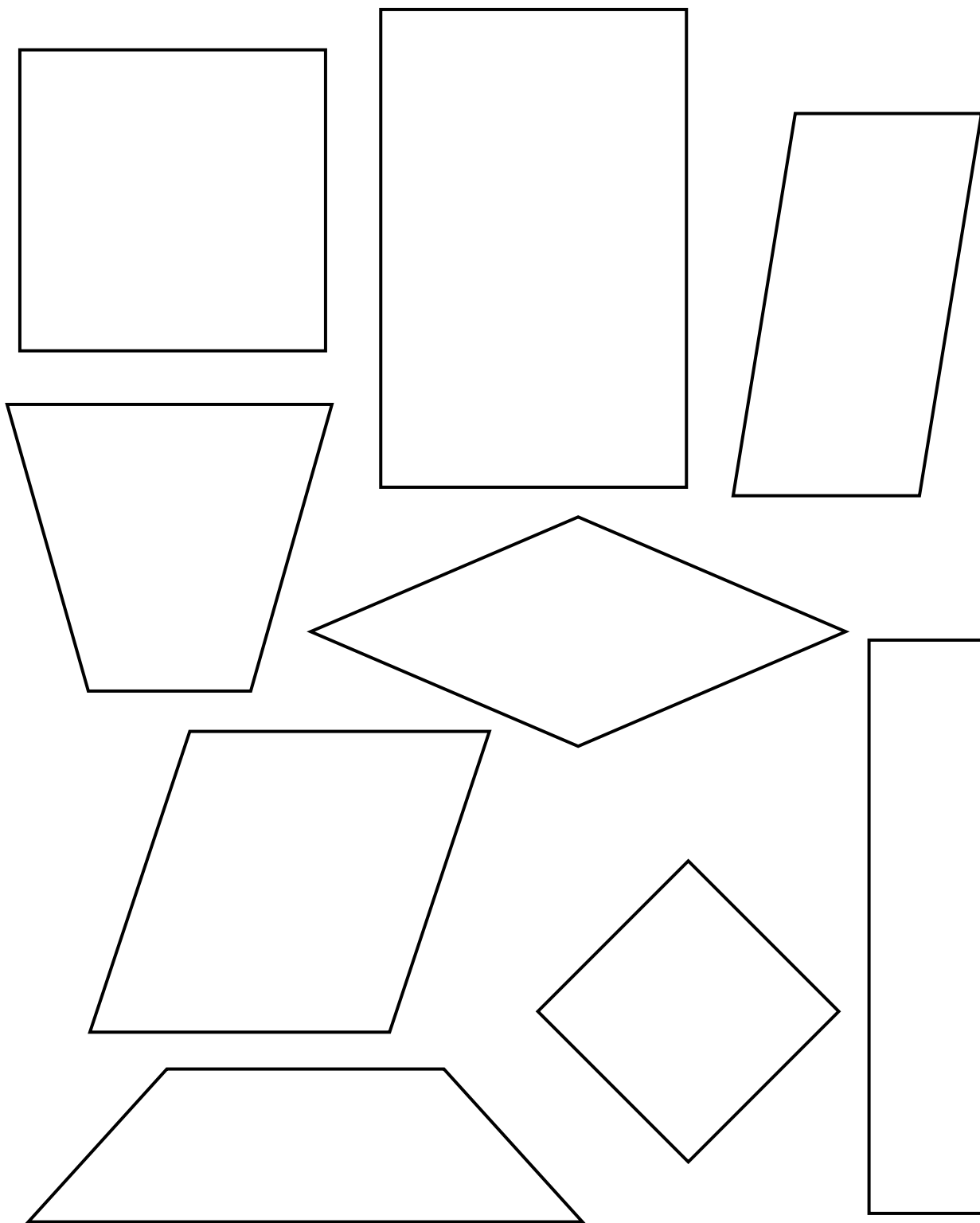
- Students that need the extension might want to compare 3 shapes using the Compare/Contrast Matrix. They may be ready for more sophisticated vocabulary to describe the sides and corners (parallel, perpendicular, right angle, obtuse angle, acute angle, line symmetry, etc.)

Intervention

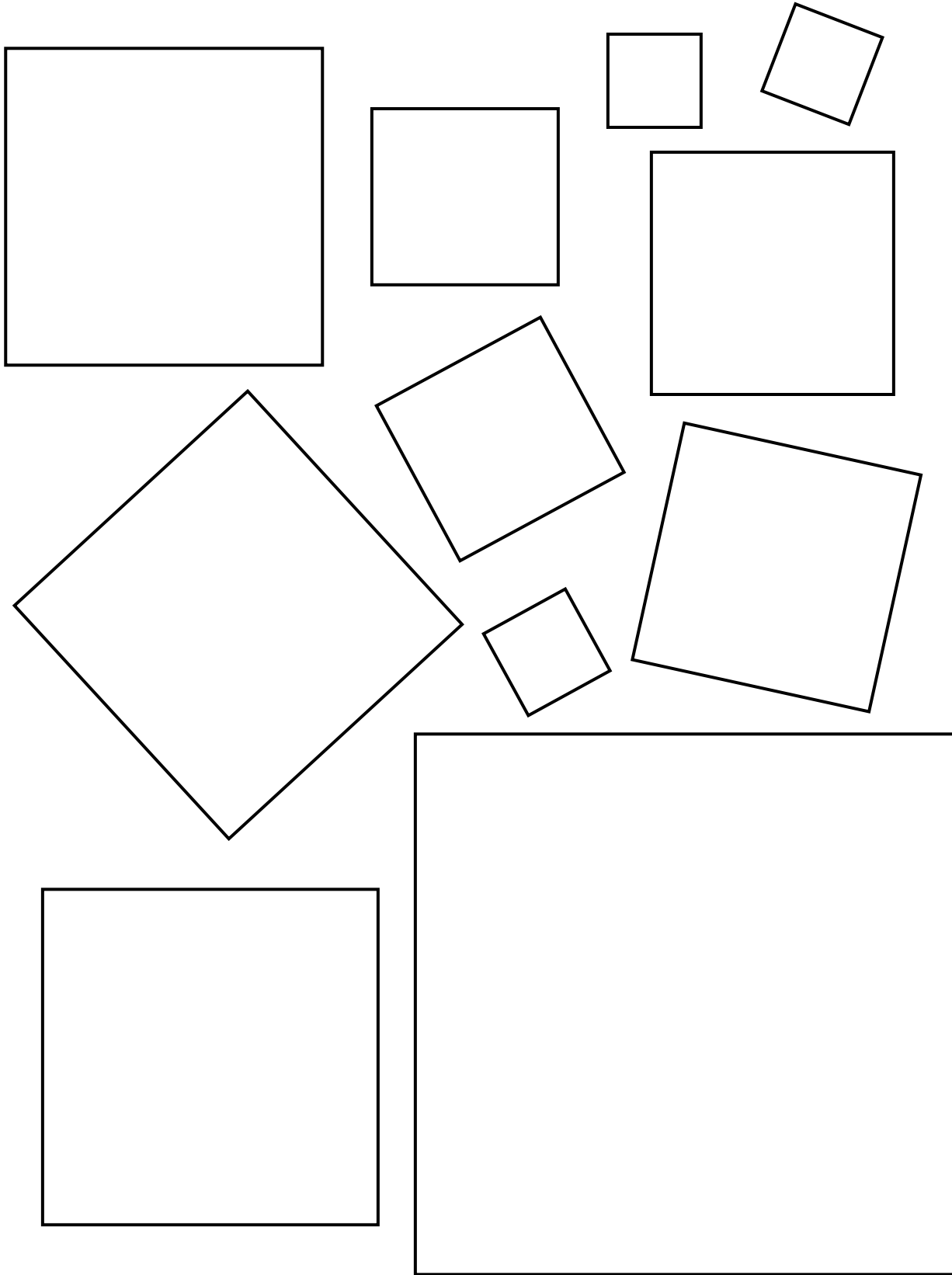
- Students that struggle with this activity are still Level 0 thinkers in the Van Hiele Levels of Geometric Thoughts. Students in this level need experiences where they can observe, feel, build (compose), take apart (decompose), or work with both two and three dimensional shapes in some manner. To help students advance, the focus should be on specific characteristics or properties to help student develop an understanding of geometric properties. Effective questioning techniques will help students clarify their thinking. Examples of questions: Can you draw a triangle that looks different than this one?  Is this rectangle  like this one ? How are they different? Explain why this shape  is like this one ? The shapes used for the sort can be used with the struggling learner for many different activities.

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CONSTRUCTION TASK: WHAT MAKES A SHAPE?



STANDARDS FOR MATHEMATICAL CONTENT

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8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students should have had experiences with common plane figures and the identification of their sides and angles. Students should also be familiar with grouping and ways to express their findings using common graphic organizers.

ESSENTIAL QUESTIONS

- How can I use attributes to compare and contrast shapes?
- Why are the properties of shapes important?
- How it is possible to have a shape that has fits into more than one category?

MATERIALS

- Small bag with a set of paper quadrilaterals for each student or pair of students
- Glue
- *The Greedy Triangle* by Marilyn Burns or other book about shape attributes
- “What Makes a Shape? Shapes for Sorting” student sheet, copied on colored paper
- “What Makes a Shape? Venn Diagram” student recording sheet, copied on white paper

GROUPING

Whole Group/Partner Task

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

In this task, students begin the process of exploring shapes for their many attributes and use critical vocabulary to describe and compare those shapes through higher-level thinking skills.

Part I

Teachers may want to begin this task by reading a book about shape attributes such as *The Greedy Triangle*. While reading, questions should be posed to the students that lead to the discovery of shape attributes – their similarities and differences. A list of attributes may be generated on the board throughout the reading or each student may be asked to keep a list of attributes. These words may already be on an anchor chart from the previous task.

Students may sort shapes by such attributes as number of vertices, or size of angles. Responses should clearly indicate how the shapes were grouped. Exemplary responses would include the use of a graphic organizer, explanations or labels that are clear, and appropriate mathematical vocabulary.

When students are working in pairs, the teacher should monitor the questioning and discussion between the students, and if necessary, model a discussion prior to or during the work time.

Once students have completed their Venn diagrams, encourage them to share their work. A few students can be selected during the work time to share their work and explain their thinking. Or if students have had experience sharing their work, they can be placed in small groups and each student can share their work with their group.

Part II

Students will follow the directions below from the “What Makes a Shape?” student recording sheet.

1. Cut out the shapes below.
2. Sort the shapes in different ways. (Use the list of attributes to help you think of different ways to sort the shapes.)
3. Choose two attributes and label the Venn diagram.
4. Sort your shapes in the Venn diagram leaving any shapes that don't fit outside of the Venn diagram.
5. Once you have checked your work, glue the shapes on the Venn diagram.
6. Write to explain your thinking and to describe any observations you made.

FORMATIVE ASSESSMENT QUESTIONS

- How could you describe this figure in relationship to another figure?
- Why did you place the figure here? (Indicate a section of the Venn diagram.)
- How do you know this shape is in the correct place?

- Choose one plane figure and tell me how it is used in the world and why its attributes are important in that use.
- Can you choose a shape not in the bag and tell me where it would fit on your paper and why?

DIFFERENTIATION

Extension

- Have students select different ways to compare/contrast the shapes, then compare their way of sorting with another student.
- Use solid figures instead of plane figures.
- Incorporate a writing opportunity by having students write a compare/contrast paragraph using 2 shapes.

Intervention

- Select a smaller sample of shapes. Provide the labels and a graphic organizer for students or do the reverse in a discovery model and set out some of the shapes in the organizer and let students determine the correct labels, then sort the remaining shapes.
- If students are having difficulty participating in productive conversations, the teacher should model using think-alouds or self-questioning strategies.

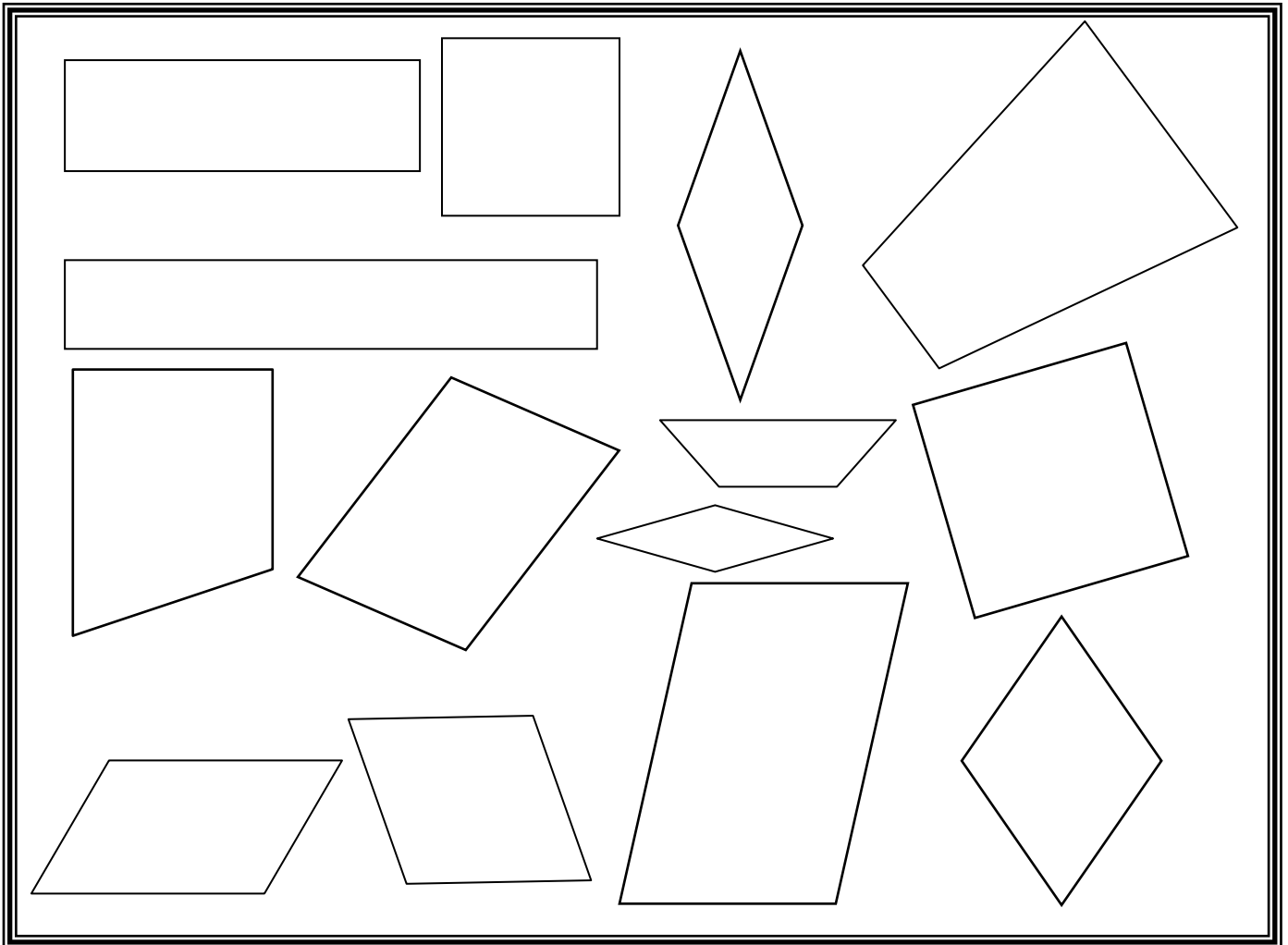
TECHNOLOGY CONNECTION

- http://nlvm.usu.edu/en/nav/frames_asid_172_g_2_t_3.html?open=activities&from=category_g_2_t_3.html Interactive geoboard from the National Library of Virtual Manipulatives
- <http://nlvm.usu.edu/>
- <http://www.mathcats.com/explore/polygons.html> - Explore Polygons
- <http://www.math-play.com/Polygon-Game.html> - Name the Shape
- http://nlvm.usu.edu/en/nav/frames_asid_170_g_2_t_3.html?open=activities&from=category_g_2_t_3.html – Compose Shapes
- http://www.learner.org/courses/learningmath/video/geometry/wmp/geo_10_k5_ch1.html - Video of teacher using Venn Diagram to sort polygons with whole class

Name _____ Date _____

What Makes a Shape?
Shapes for Sorting

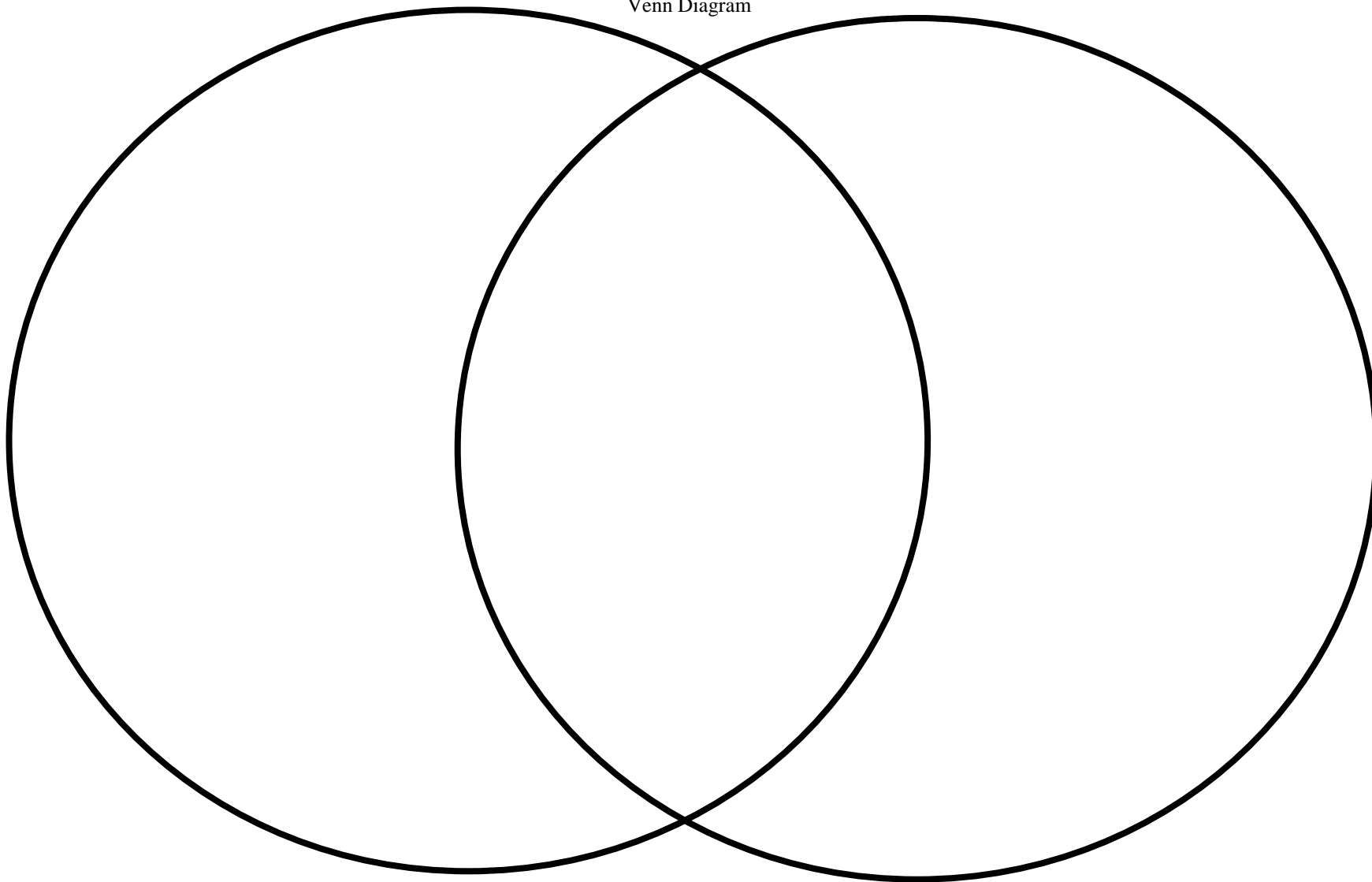
1. Cut out the shapes below.
2. Sort the shapes in different ways. (Use the list of attributes to help you think of different ways to sort the shapes.)
3. Choose two attributes and label the Venn diagram.
4. Sort your shapes in the Venn diagram leaving any shapes that don't fit outside of the Venn diagram.
5. Once you have checked your work, glue the shapes on the Venn diagram.
6. Write to explain your thinking and to describe any observations you made.



Name _____ Date _____

What Makes a Shape?

Venn Diagram



CONSTRUCTING TASK: PROPERTIES OF QUADRILATERALS

Adapted from Property Lists for Quadrilaterals Van de Walle Activity 8.8

STANDARDS FOR MATHEMATICAL CONTENT

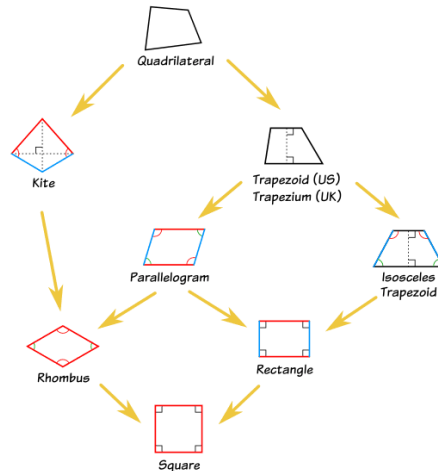
MCC3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Throughout this unit, the goal for third grade students is to begin to understand that quadrilaterals are all four sided closed polygons. While angles and lines have not been studied yet (this will be addressed in 4th grade standard CCM4.G.1), it is important for students to begin to see that the angles can be square (right), skinny (acute) or fatter than a square (obtuse). Use index cards, set squares, or corners of paper to compare angles. Accept terms students use as a teachable moment, when appropriate. The same applies with talking about the sides. Students may say opposite sides or the sides that run into each other. Within the broad category of quadrilaterals are trapezoids, parallelograms, rhombuses, rectangles, and squares. Through many activities, students need to begin to understand the categories of two-dimensional shapes (see Van de Walle page 221 for descriptions).



For Teacher Reference ONLY – Taken from

<http://www.regentsprep.org/regents/math/geometry/GP9/LQuad.htm>

Quadrilateral: A quadrilateral is any four sided figure. Do not assume any additional properties for a quadrilateral unless you are given additional information.

Trapezoid: A trapezoid has **ONLY ONE** set of parallel sides. When proving a figure is a trapezoid, it is necessary to prove that two sides are parallel and two sides are not parallel

Parallelogram: A parallelogram has 2 sets of parallel sides, 2 sets of congruent sides, opposite angles congruent, consecutive angles supplementary, diagonals bisect each other and the diagonals form 2 congruent triangles

Rectangle: The rectangle has all of the properties of the parallelogram, **PLUS** 4 right angles, and diagonals congruent

Rhombus: The rhombus has all of the properties of the parallelogram, **PLUS** 4 congruent sides, diagonals bisect angles, diagonals perpendicular

Square: The square has all of the properties of the parallelogram **AND** the rectangle **AND** the rhombus.

ESSENTIAL QUESTIONS

- Is it possible for a square to be a rectangle?
- Why do some quadrilaterals look so much alike?
- Is a rectangle a rhombus?
- Can some shapes be called other names?

MATERIALS

- Student Recording Sheet
- Index Cards (used to compare angles and sides)

GROUPING

Partner or Group

TASK DESCRIPTION, DEVELOPMENT , AND DISCUSSION

In this task, students will look at examples of rhombuses, rectangles, and squares to make property lists of quadrilaterals. Students will use the index card to check angles, compare side lengths and draw lines if needed. Encourage students to use “at least” when describing how many of something the shape has. For example, a rectangle has at least 4 square corners. Have students compare sides (length), and angles (square, smaller than square, larger than square). Some students may begin to see diagonals and symmetries of the shapes. Have groups share what they discovered together (remember that defending arguments and critiquing the reasoning of others is a major part of mathematic instruction!) and create a class list for each shape.

FORMATIVE ASSESSMENT QUESTIONS

- Did you notice anything particular about squares?
- How do you know that a quadrilateral is a rhombus or a rectangle?
- Why do you think that a rectangle, rhombus, and a square are all parallelograms?
- Is a trapezoid also a parallelogram?

DIFFERENTIATION

Extension

- As this task exists currently, it is considered to be at level 1 of the van Hiele geometric thinking, which is appropriate for third grade. According to Van de Walle, most fourth and fifth graders will still be at a level 0 or 1. Students that need an extension might consider doing Activity 8.11 called Minimal Defining Lists on page 230 or Activity 8.12 called True or False? On page 231 in the 3-5 Van de Walle resource book.

Intervention

- This task will be difficult for the majority of your students. By working with a partner, the struggling learner can begin to understand that some shapes fit into several categories because of the properties that they share. For instance, a square is a rectangle, a rhombus, a parallelogram and a quadrilateral because it shares properties. Many examples may need to be provided for the struggling learner. Technology can provide many opportunities for the student. See Technology Connections.

TECHNOLOGY CONNECTIONS

- <http://www.mathsisfun.com/geometry/quadrilaterals-interactive.html> - allows students to move corners to make sizes.
- <http://www.interactivestuff.org/match/maker.phtml?featured=1&id=24> – matching game
- http://www.mathplayground.com/matching_shapes.html - matching games (includes kite)

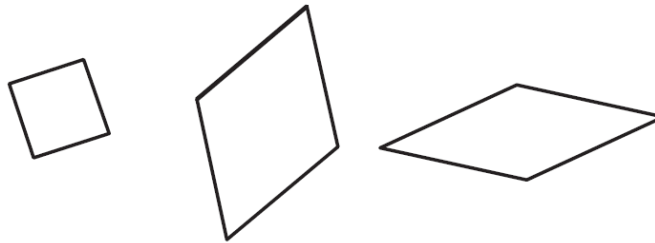
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Date: _____

Quadrilaterals

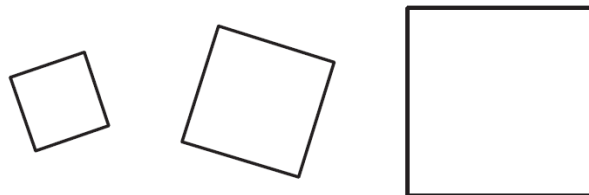
Directions: Look at of the different shapes. Write down anything you notice about the type of shape. Look at the corners (angles) and the sides. Use an index card corner (square corner) to write down what you notice about the corners. Also use the index card to help you measure the length of the sides. Begin to define rhombus, square, rectangle and parallelogram.

These are all rhombuses.



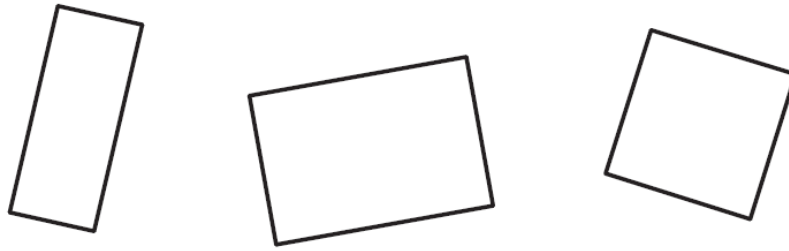
Observations about rhombuses

These are all squares.



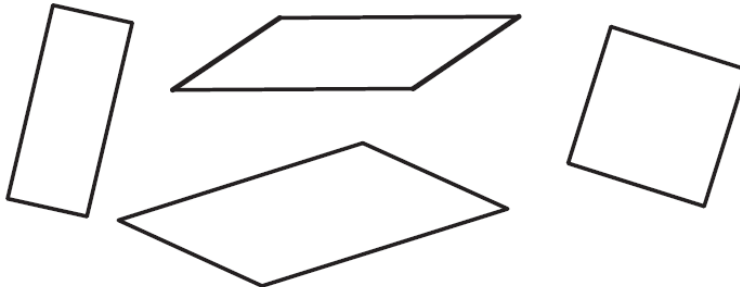
Observations about squares

These are all rectangles.



Observations about rectangles.

These are all parallelograms.



Observations about parallelograms.

PRACTICE TASK: CAN YOU FIND IT?

Adapted from North Carolina Math Instructional Resources

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students often have trouble seeing shapes within other shapes. They also have a difficult time if the shape is a different orientation than is seen most often. Most students will be able to draw the shapes requested. For those that struggle, provide models of the shapes requested.

ESSENTIAL QUESTIONS

- What are some ways that a hexagon (or pentagon) can look?
- Do rectangles and squares always look the same?
- Does the direction that a shape is facing change the way it looks? Does it change the shape's name?


MATERIALS

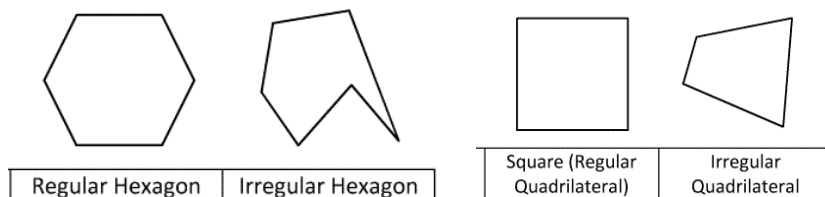
- Can You Find It? Student Resource Sheet or http://wps.ablongman.com/wps/media/objects/3464/3547873/blackline_masters/BLM_40.pdf
- Color pencils or crayons

GROUPING

Individual or Partner

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

You may wish to open this lesson by reading a book such as *Shape Spotter* by Megan Bryant, *The Story of Goldie Locks and the Three Squares* by Grace Maccarone, or a similar book. Then, students will use the *Can You Find It?* student resource sheet to locate a rectangle, square, triangle, hexagon, pentagon, a quadrilateral that does not look like a rectangle or square, trapezoid, rhombus, a different looking hexagon, and a different looking trapezoid. They may color each shape a different color and then put some type of marking on all of the quadrilaterals, or you may want them to color all quadrilaterals the same color. Many students struggle to see irregular shaped polygons as fitting into the category with the regular shaped polygons. For instance, most students only know that a hexagon looks like  but a hexagon is **any** six sided closed figure. An important part of the task is to allow students to compare their drawings. This will help students who struggle with orientation of shapes.





FORMATIVE ASSESSMENT QUESTIONS

- Did all of your quadrilaterals have a square corner?
- Do all of your shapes look like a classmate's shapes? How were they different? How are they alike? What attributes help you know that the shapes are still the same?
- How do you know you drew a square and a rhombus?

DIFFERENTIATION

Extension

- Students who need an extension can draw different quadrilaterals and label them. They could also try drawing the shapes in a different orientation or direction. For example, if the trapezoid looks like  , have students draw the trapezoid like .

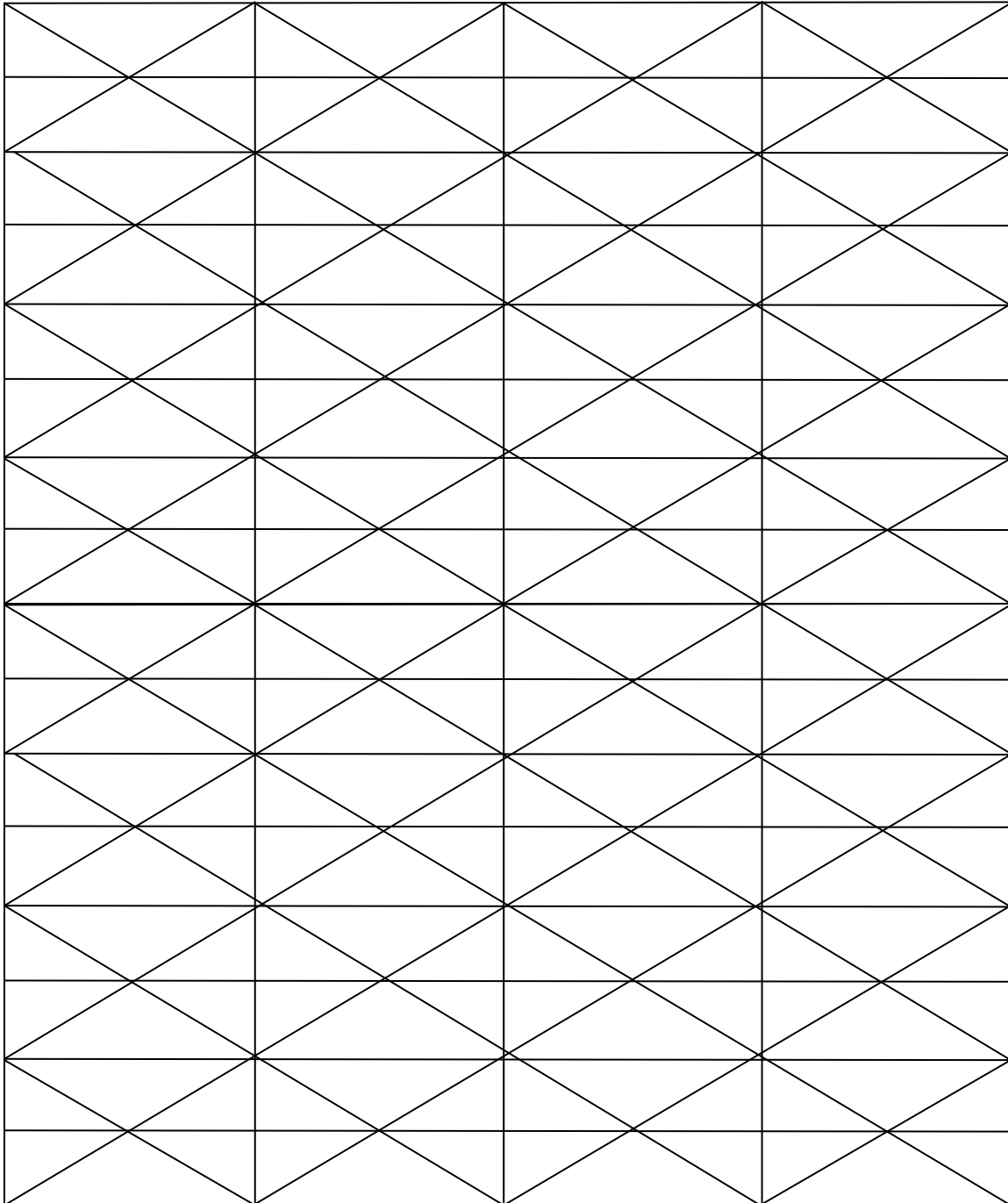
Intervention

- Provide models of the shapes for students to be able to place on the grid to trace around. Remind students that shape names also tell the number of sides. For instance, a quadrilateral is any closed figure with 4 sides and a hexagon means any closed figure with 6 sides.

CAN YOU FIND IT?

Find the shapes listed below. Once you find it, use different colors to shade in or trace around the shape. Also color code the directions.

<ul style="list-style-type: none">• Rectangle• Square	<ul style="list-style-type: none">• Triangle• Hexagon• Pentagon	<ul style="list-style-type: none">• Quadrilateral that does not look like a Rectangle or Square• Trapezoid• Rhombus	<ul style="list-style-type: none">• A Different looking Trapezoid• A Different looking Hexagon
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PRACTICE TASK: SCORE IT!

Adapted from NC Math and from <http://nrich.maths.org/191>

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

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8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students often struggle with finding shapes if the shape looks different than what is typical seen. In this activity, students are encouraged to find the triangles, quadrilaterals, pentagons, and hexagons seen in two different figures. This will help to continue to build student's spatial sense and geometric reasoning. It takes many experiences with shapes to be able to further develop these skills with students.

ESSENTIAL QUESTIONS

- How might finding shapes within other shapes help me in life?
- Can you provide an example of a non-regular pentagon or hexagon?
- Do quadrilaterals have to look like rectangles? How do you know?

MATERIALS

- Printed copies of the student sheet OR use technology to display student sheet
- Math Journal or paper to keep track of number of shapes and total score

GROUPING

Individual or Partner

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

This is a practice task that could be included in a center or small group activity where all students are not working on it at the same time. In Figure A, students will review the properties of triangles, quadrilaterals, pentagons, and hexagons as they find the shape within the figure. In Figure B, students will locate all of the rectangles and squares within the figure. Some students might be able to solve this by simply tracing over the shape with their pencils. Others might need to draw the shapes on paper. For the struggling student, you may want to get tracing paper or lightweight paper to have students trace over the lines to find all of the shapes.

FORMATIVE ASSESSMENT QUESTIONS

- How could you make sure you find all of the shapes within other shapes?
- How do you think this type of task helps you for the future?
- Do you struggle with finding shapes that are irregular?

DIFFERENTIATION

Extension

- Allow students to create another type of figure like either A or B. Once they know how many shapes are in their large shape, allow other students to solve for the answer. You may also want to visit Figure 8.6 on page 216 of the Van de Walle resource to have students make different shapes with the mosaic puzzle that is in the black line masters. There are several different rectangle and parallelograms that could be created.

Intervention

- Suggestions: Tracing paper or lightweight paper to trace the lines; colored pencils and have student change colors for each type of shape; allow student to have their own copier paper that has either figure multiple times (to cut out or trace over)

Name _____ Date _____

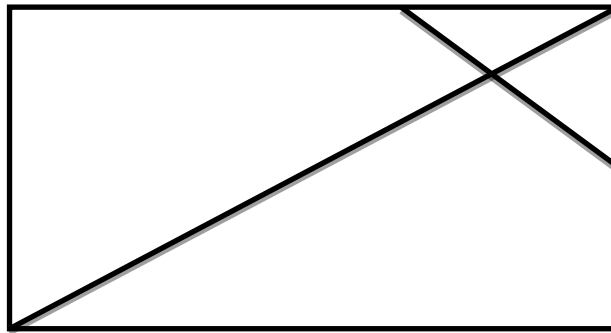
Score It!

Direction: Use Figure A and find all of the triangles, quadrilaterals, pentagons and hexagons. Once you believe you have found all of the shapes, give the appropriate amount of points to each shape found. Find the highest possible score. Once you have it, compare your score to the others in your group. Is it different? Why?

Score This Figure:

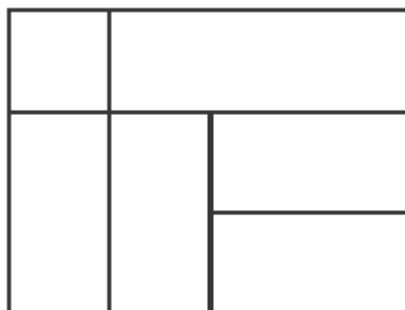
- 2 points for Triangles
- 3 points for Quadrilaterals
- 4 points for Pentagons
- 5 points for hexagons

Figure A

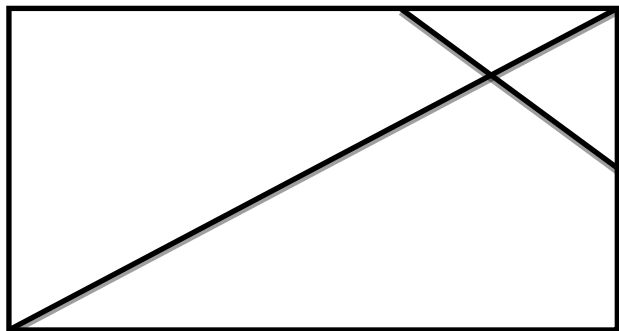
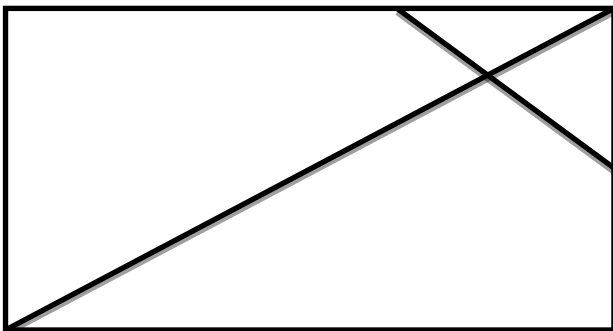
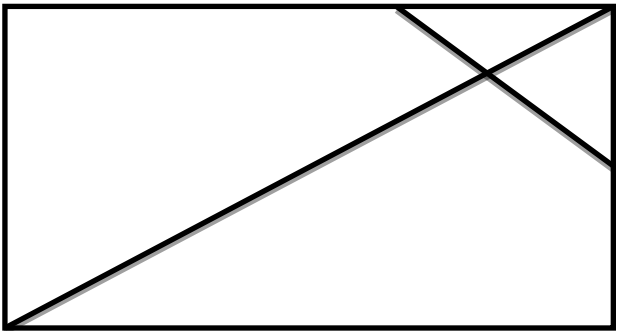
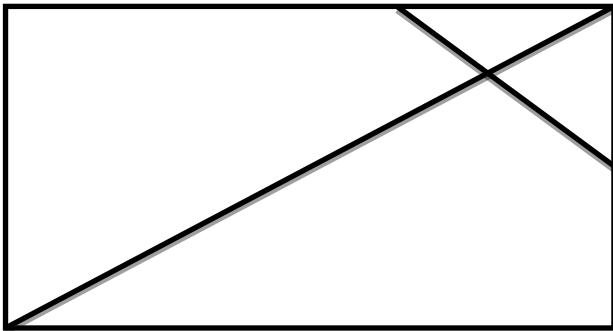
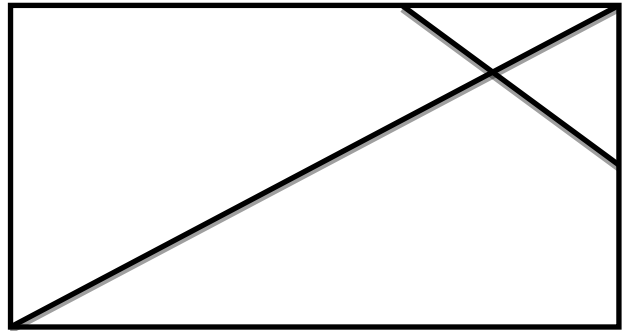
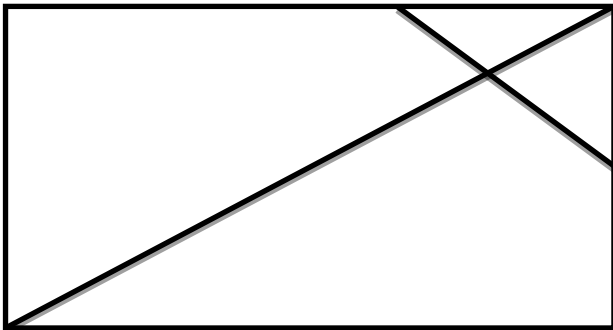
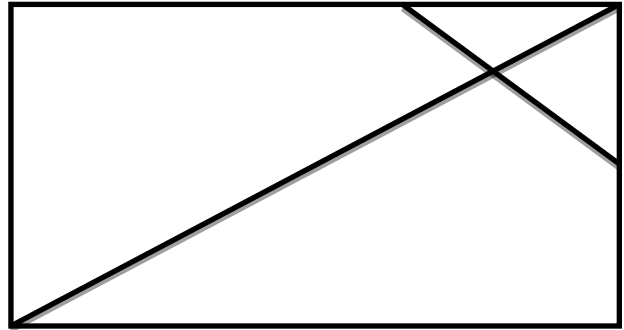
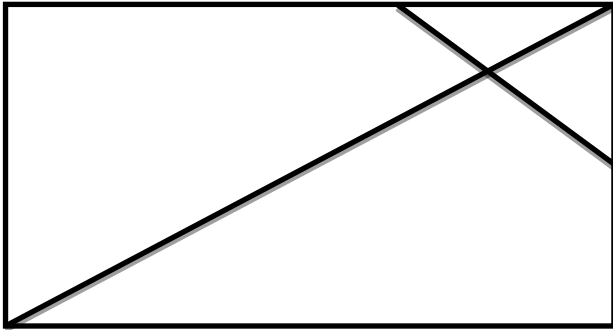


Directions: Use Figure B and find all of the rectangles. Remember what you have learned about rectangles and squares. Do you see any shapes that are similar to each other?

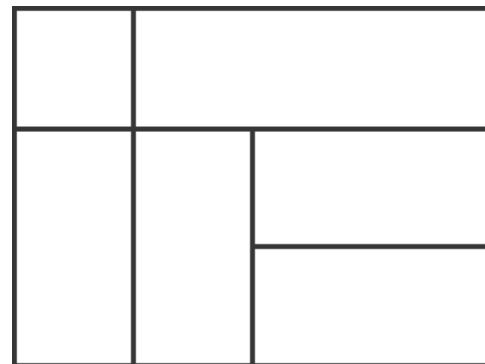
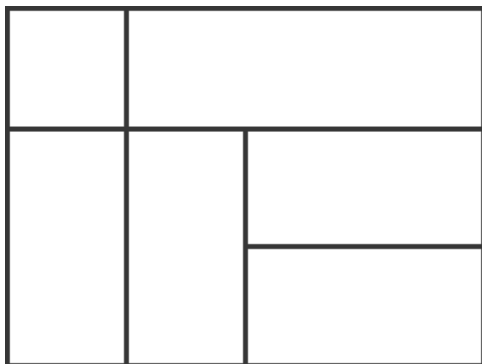
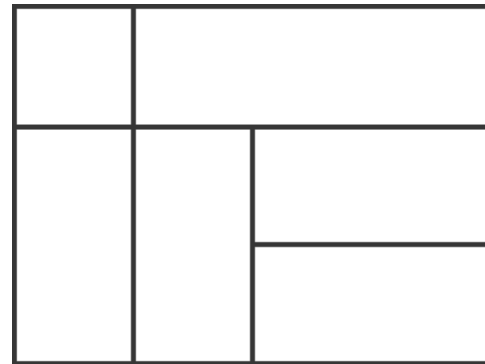
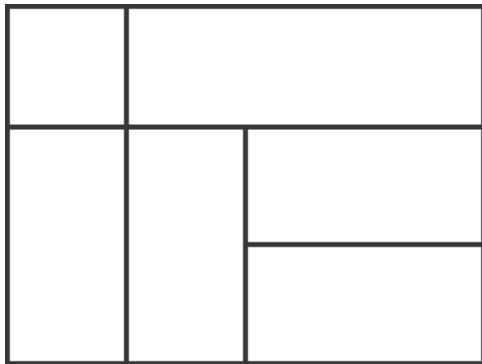
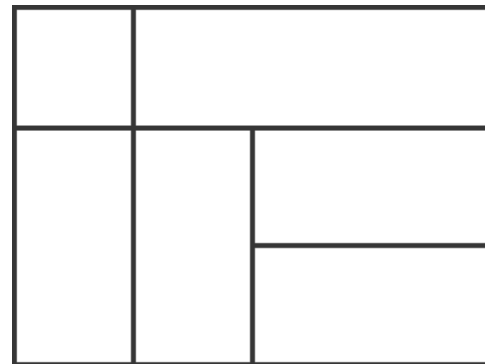
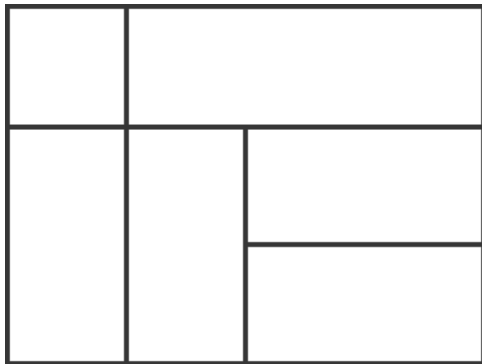
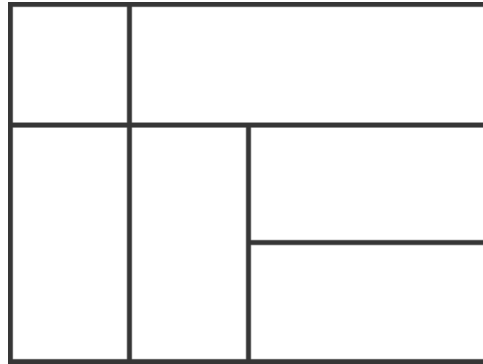
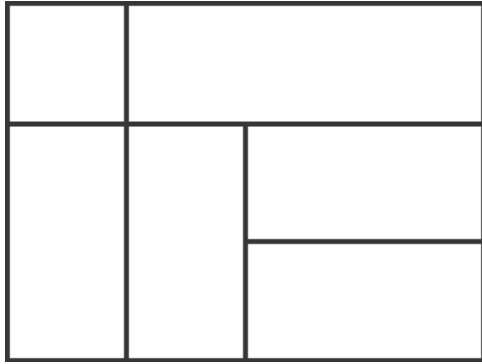
Figure B



Copier Sheet: Print to give each student their own copy of the design.

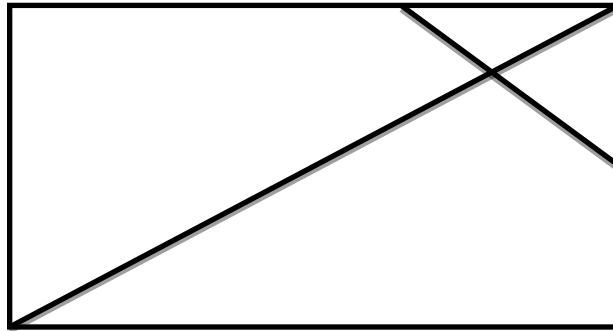


Copier Sheet: Print to give each student their own copy of the design.



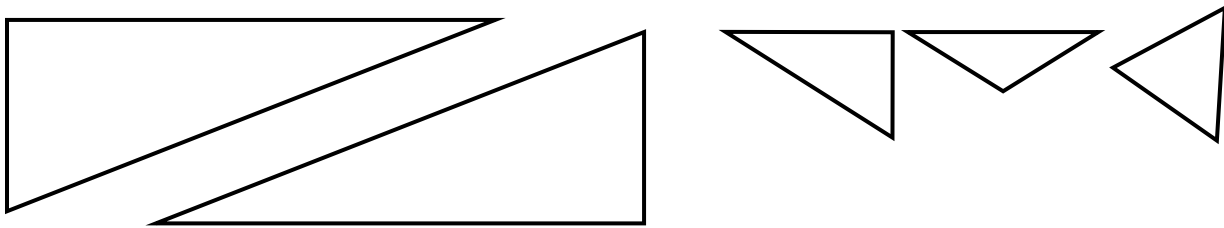
Teacher Answer Key for Figure A:

Figure A:

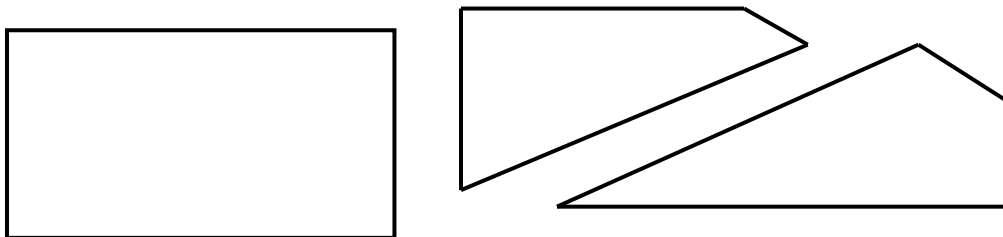


There are 5 triangles, 3 quadrilaterals, 3 pentagons, 2 hexagons for a total of 41 points.

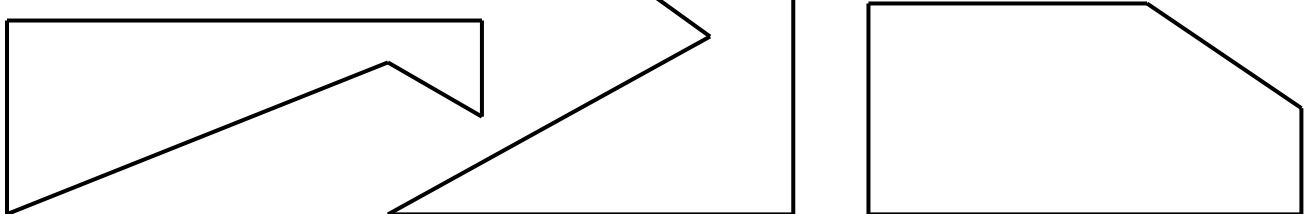
Triangles:



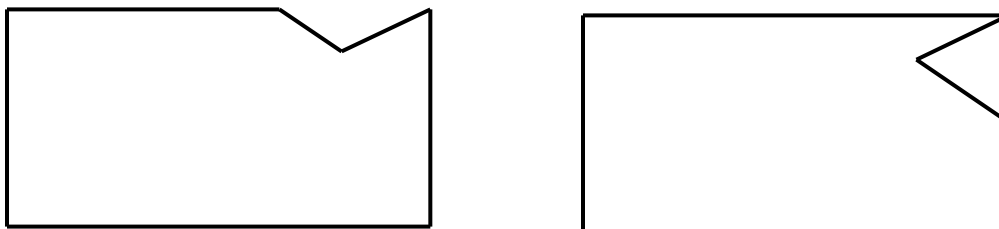
Quadrilaterals:



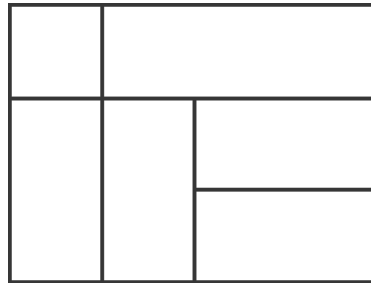
Pentagons:



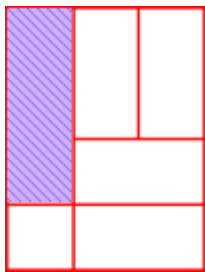
Hexagons:



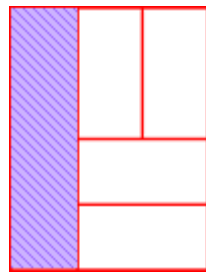
Teacher Answer Key for Figure B:



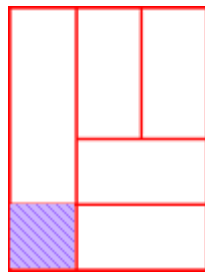
14 solutions



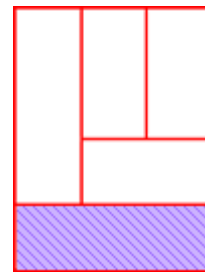
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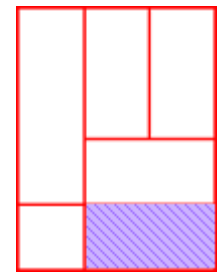
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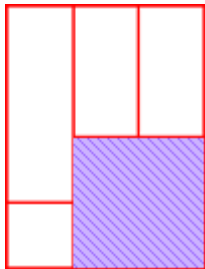
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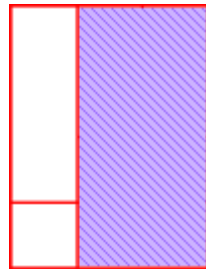
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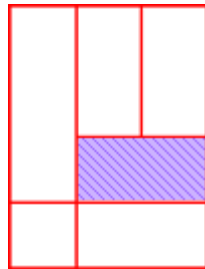
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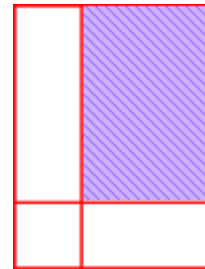
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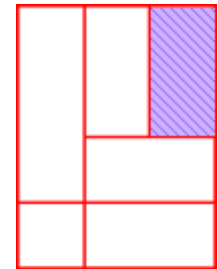
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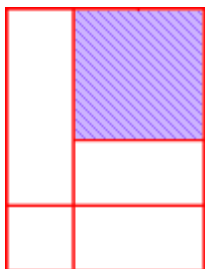
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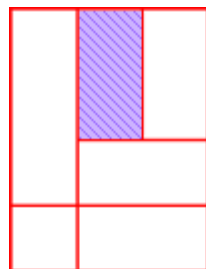
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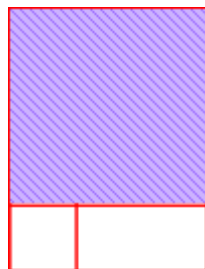
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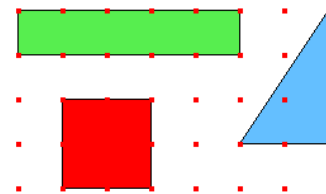


14

CONSTRUCTING TASK: GEOBOARD GEOMETRY GURU

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.



MCC3.G.2 Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.*

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND

Students should begin to use what they have learned about properties from the previous activities to be able to begin to classify shapes. Begin with shapes learned in previous grades and move up to focusing on quadrilaterals.

Before beginning this task, students should be familiar with common quadrilaterals and the identification of their sides and angles. Also, they should be able to use a geoboard and transfer that information to paper. Some students may need specific instructions on how to transfer figures to the paper (e.g. counting the spaces between dots and directionality). Finally, students should be able to make multiple representations of the same shape with variance in size and orientation, and still determine it to be the same shape based on its attributes.

ESSENTIAL QUESTIONS

- How can I use attributes to compare and contrast shapes?
- Is it possible to make shapes that are quadrilaterals that are not shaped like what I might be used to?

MATERIALS

- Geoboards
- Rubber bands
- “Geoboard Geometry Guru” student recording sheet (3 per student)

GROUPING

Whole Group/Individual Task

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I

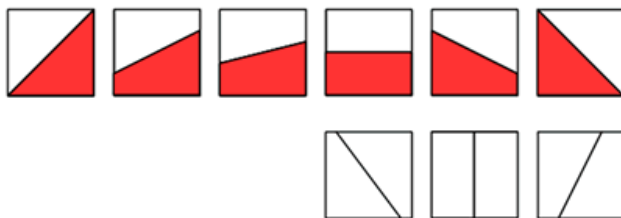
In this task, students begin exploring how to create plane figures using straight lines and angles and then discover common features of rectangles, squares, and triangles.

Students should be given the opportunity to explore freely with the geoboard and rubber bands before working this task. Also, teachers may want to begin this task by giving students opportunities to explore the geoboard by making a variety of shapes, lines, and angles. Throughout this task teachers should promote the key vocabulary of open figure, closed figure, polygon, rhombus/rhombi, rectangle, square, quadrilateral, parallelogram, and trapezoid. Also, students should be encouraged to use these key vocabulary words.

At the completion of this task the class will have created definitions for rectangle, square, rhombus, and trapezoid. These can be posted in the classroom along with each shape’s attributes.

Part II

Have students return to the geoboard and begin to explore partitioning the shapes into equal parts. Is it possible to make all of the quadrilaterals into equal parts of two, three, four, six, and eight? Guide students through making sense of equal parts/areas. An anchor chart may be drawn to show how each quadrilateral can be partitioned into equal areas. Remember that each shape can be partitioned in multiple of ways. For instance, a square can be divided into half in all of these different directions:



Task Directions

Students should be challenged to make different shapes that describe one or more properties of shapes. Pose questions to students like: Can you make a shape with just one square

corner and four sides? Can you make a shape with 2 square corners (or 3, 4, 5, etc. square corners?) Can you make a shape that has two pairs of sides that go the same way or are parallel? Show student’s examples so that students can begin to understand that there is more than one way to make a shape with the same properties. The focus should be on looking at the different quadrilaterals that can be created. Students are asked to create all of the different rectangles they can find on the geoboard and then record them on geoboard paper. Ask students to say aloud or write as many complete sentences as they can that begin with “All (or none, or some) of the rectangles....” in order to draw general conclusions about the shapes. After general conclusions have been stated or recorded, the teacher can lead the students to create an appropriate definition for a rectangle.

Follow the same procedures to create an appropriate definition for a square, rhombus, parallelogram, and trapezoid (review from 2nd grade). Note: This activity might take more than 1 day in order for students to get to explore each shape and think about what makes each shape different. For a more descriptive table, please see Table 8.1 “Categories of Two- Dimensional Shapes” on page 221 and Figure 8.11 “Classifications of Two-Dimensional Shapes” in the 3-5 Van de Walle text, page 222.

Shape		Description
Classified by sides	Equilateral	All sides are congruent.
	Isosceles	At least two sides are congruent.
	Scalene	No two sides are congruent.
Classified by angles	Right	Has a right angle
	Acute	All angles are smaller than a right angle.
	Obtuse	One angle is larger than a right angle.
Quadrilaterals		Polygon with exactly four sides
Trapezoid		At least on pair of parallel sides
Parallelogram		Two pairs of parallel sides
Different Classes of Parallelograms	Rectangle	Parallelogram with a right angle.
	Rhombus	Parallelogram with all sides congruent
	Square	Parallelogram with a right angle and all sides congruent.

In addition to recording the defining properties, the shapes that students have drawn on the geopaper might be used as a formative assessment for MCC3.G.2. Have students use the drawn shapes or the geoboards to show what they know about partitioning a shape into halves, thirds, fourths, sixths and eighths. Allow students to show a variety of ways to partition the shapes. It is important that students continue to develop their understanding of equal areas. More activities will follow that continue the exploration for MCC3.G.2

FORMATIVE ASSESSMENT QUESTIONS

- What is your definition of a rectangle (or square, rhombus, trapezoid, or parallelogram)?
- What are the attributes of a rectangle (or square, rhombus, trapezoid, or parallelogram)?
- How can you change this shape by changing only one attribute?

- Is this shape still a (rectangle..or any shape) if I turn the geoboard slightly? (Look to see if orientation confuses students)
- Show half (or thirds, fourths, sixths, eighths) in a different way.

DIFFERENTIATION

Extension

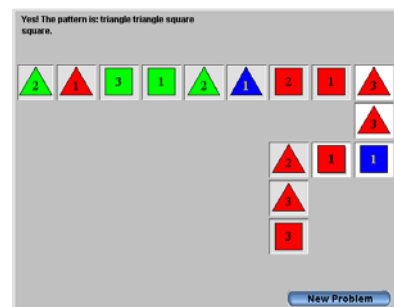
- Have students create a morph chain of a shape changing one attribute at a time and label each morphed shape with its description. (For example: small, red equilateral triangle morphs into a small, blue, equilateral triangle and then into a small, blue, isosceles triangle, etc.)

Intervention

- Provide the definition of the shape first and deconstruct the definition while creating each part of the shape until the shape is complete. Then have students create a congruent shape. Finally ask students to create a non-congruent shape, changing one attribute.

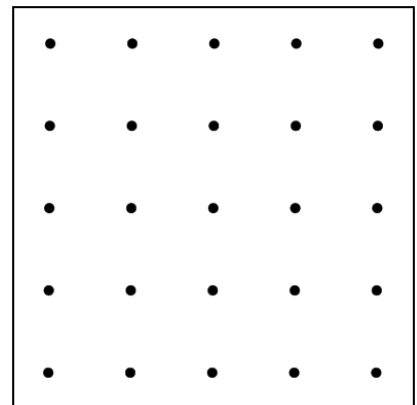
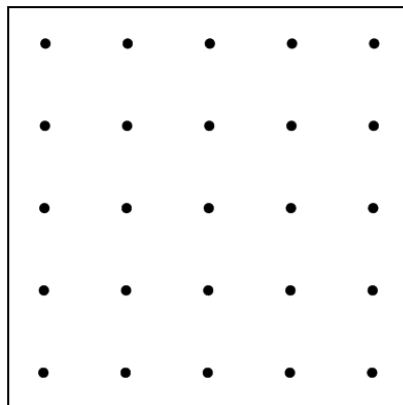
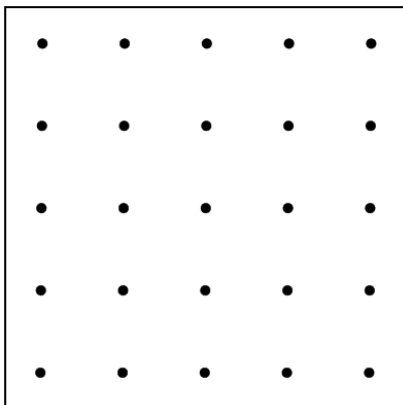
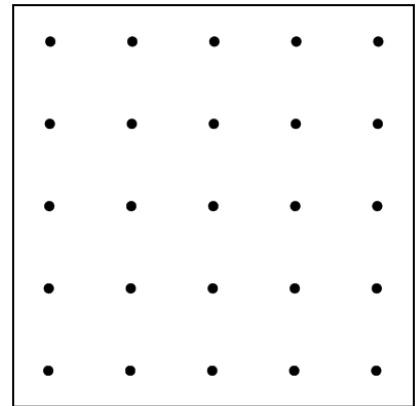
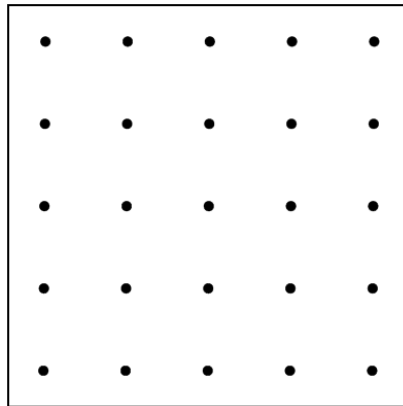
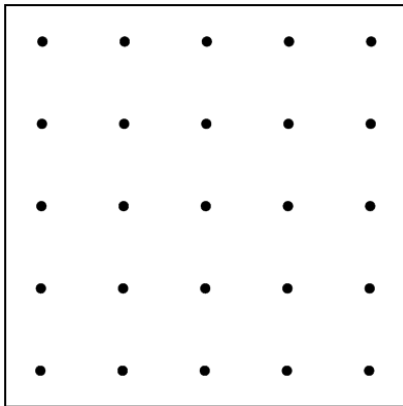
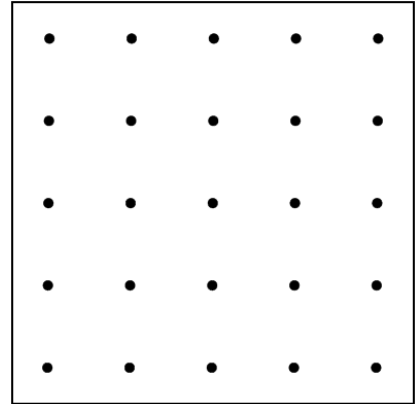
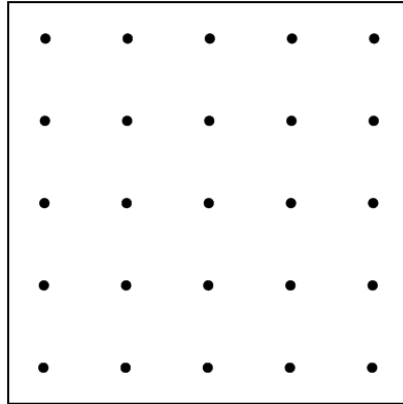
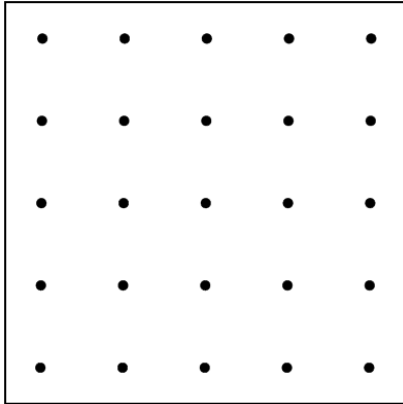
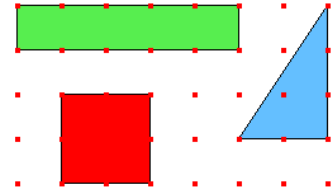
TECHNOLOGY CONNECTION

- http://nlvm.usu.edu/en/nav/frames_asid_172_g_2_t_3.html?open=activities This site offers an easy to use virtual geoboard.
- http://nlvm.usu.edu/en/nav/frames_asid_271_g_2_t_3.html?open=instructions&from=category_g_2_t_3.html Students follow a pattern to create attribute trains based on color, shape, or the number on the shape (e.g. triangle, square pattern; red, red, blue pattern; triangle, square, square pattern; 2,3,1 pattern).



Name _____ Date _____

Geoboard Geometry Guru



CONSTRUCTING TASK: QUADRILATERAL CHALLENGE

Adapted from a lesson by Amanda Grant, Eagle Springs ES, Houston County Schools

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

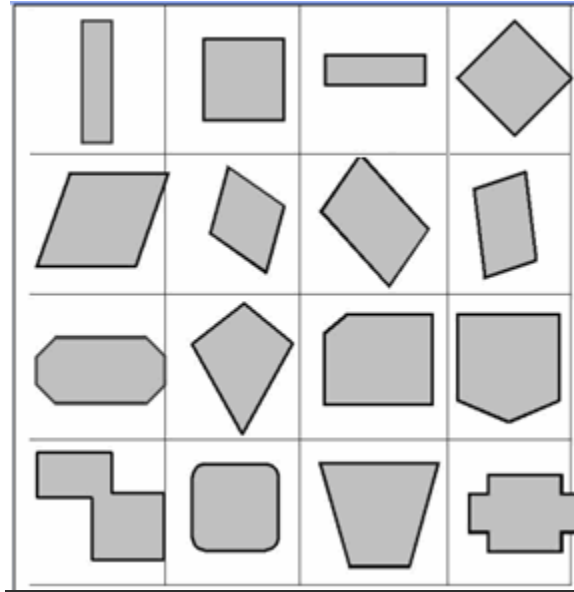
BACKGROUND KNOWLEDGE

Students should have the following background knowledge about quadrilaterals.

- Understand that opposite sides can not touch each other; they are on opposite sides of the quadrilateral.
- Understand that shapes can be described by the attributes and properties that it has.
- Know that a property is an attribute of a shape that is always going to be true. It describes the shape.
- Be able to use a ruler to measure sides to verify they are the same length.

Students should have some experience with the properties of quadrilaterals as shown in the diagram below.

Students who are not clear on the important features of rectangles (four straight sides and four right angles) may not realize that the shapes in the first row are all rectangles, while none of the shapes in the other rows are rectangles. Note that two of the rectangles in the first row are 'special rectangles'; as well as having four straight sides and four right angles, the four sides are the same length, so these special rectangles are known as squares.



Recognizing parallelograms

In the diagram above, the second row contains four 'pushed over rectangles' or 'parallelograms'. These four-sided shapes are similar to rectangles in that the opposite sides are the same length, but the angles are not right angles.

Of the four parallelograms in the second row, the first two have equal-length sides and so are 'special parallelograms' known as rhombuses. They could also be thought of as 'pushed over squares'.

ESSENTIAL QUESTIONS

- What is a quadrilateral?
- How can you create different types of quadrilaterals?
- How are quadrilaterals alike and different?
- What are the properties of quadrilaterals?

MATERIALS

For Each Group:

- “Quadrilateral Challenge, Quadrilateral Mat” student recording sheet (print on legal-size paper)
- “Quadrilateral Challenge, Quadrilateral Properties” student sheet (One sheet for every two groups; cut along dotted line; print on colored paper)
- Rulers
- Index cards
- Scissors
- Glue sticks
- Wikki Sticks (optional, approximately five sticks per group) OR dot paper

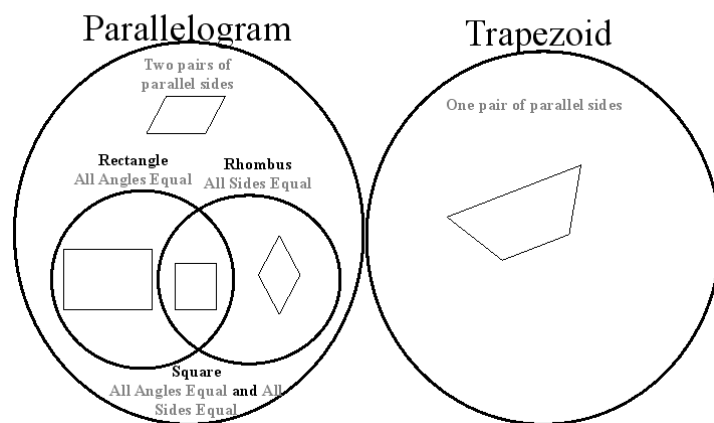
- “Quadrilateral Challenge, Dot Paper” student recording sheet (optional)

Comments

Students will need Wikki Sticks, toothpicks or plastic coffee stirrers with modeling clay, or other materials with which to create their quadrilaterals) OR the “Quadrilateral Challenge Dot Paper” student recording sheet so that students can use to draw, cut out, and glue their quadrilaterals to their “Quadrilateral Mat.”

Copy the “Quadrilateral Mat” student recording sheet onto white paper. To contrast the white paper, the “Quadrilateral Properties” student sheet should be copied onto **colored paper**; otherwise crayons need to be provided so that students can color the quadrilaterals before they cut them out.

Quadrilaterals



GROUPING

Partner/Small Group Task

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

The purpose of this task is for students to become familiar with the properties of quadrilaterals. Working in pairs, students will create the following quadrilaterals: parallelogram, rhombus, square, rectangle, trapezoid. They will identify the attributes of each quadrilateral, then compare and contrast the attributes of different quadrilaterals.

Students will work in pairs. They will first construct an example of each quadrilateral (square, rectangle, trapezoid, and rhombus) on their quadrilateral mats. After they have created each quadrilateral, the students will determine the properties of each figure by sorting the property cards. Students need to sort all of the property and picture cards and match them to the correct quadrilateral before they glue the cards underneath the figures that they have created.

Once students finish their Quadrilateral Mats, students should choose 2 quadrilaterals and write to compare and contrast their properties.

Some properties of quadrilaterals that should be discussed are included below. As students draw conclusions about the relationships between different figures, be sure they are able to explain their thinking and defend their conclusions.

- A shape is a quadrilateral when it has exactly 4 sides and is a polygon. (To be a polygon the figure must be a closed plane figure with at least three straight sides.)
- A square is always a rectangle because a square will always have 4 right angles like a rectangle.

- A rectangle does not have to have 4 equal sides like a square. It can have 4 right angles without 4 equal sides. Therefore, rectangle is not always a square.
- A square is always a rhombus because it has 4 equal sides like a rhombus and it is also a rectangle because it has 4 right angles like a rectangle.
- A rhombus does not have to have right angles like a square. It can have 4 equal sides without having 4 right angles. Therefore, a rhombus is not always a square.
- A trapezoid can never be a parallelogram because a trapezoid has only one pair of opposite sides that are parallel and a parallelogram has two pairs of opposite sides parallel.
- A parallelogram can be a rectangle if it has 4 right angles.

Task Directions

Students will create at least one quadrilateral (using a material such as Wikki Sticks, toothpicks/straws and modeling clay, or dot paper) for each section of the “Quadrilateral Mat” Then students will cut, sort, and glue the properties and pictures for each quadrilateral from the “Quadrilateral Properties” student sheet (**Note: only 1 sheet is needed for every 2 students**). Finally, students will write to compare and contrast the properties of two quadrilaterals.

FORMATIVE ASSESSMENT QUESTIONS

- How do you know this quadrilateral is a _____ (square, rectangle, trapezoid, or rhombus)?
- How did you create your quadrilaterals?
- Is there a quadrilateral that was easier/harder to create than others? Why?
- How do you know these are quadrilaterals?
- How are quadrilaterals different from other 2-D shapes? How are they the same?
- What is meant by the term “opposite sides”?
- How can you show that 2 sides are equal?
- What are some ways we can show an angle is a square or right angle?

DIFFERENTIATION

Extension

- Ask students to create a Venn diagram which contains a comparison of the properties of two quadrilaterals.

Intervention

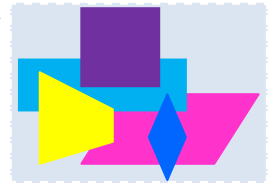
- Allow students to list similarities and differences of two quadrilaterals rather than write a paragraph.
- Help students organize the quadrilateral properties before placing them on the mat. There are several that are the same. Have students place like properties in a pile and then decide which shape has that particular property. Place all of one property on the mat before moving to another property.

TECHNOLOGY CONNECTION

- <http://www.regentsprep.org/regents/math/geometry/GP9/LQuad.htm> A summary of the properties of several quadrilaterals.
- http://teams.lacoe.edu/documentation/classrooms/amy/geometry/6-8/activities/new_quads/quads.html A virtual “Quest” where students match properties with quadrilaterals.
- <http://www.shodor.org/interactivate/lessons/IntroQuadrilaterals/> An introduction to Quadrilaterals
- <http://www.mathsisfun.com/quadrilaterals.html> - Use after completing the Quadrilateral Challenge; does allow for students to move the corners of the quadrilaterals


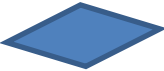






My Quadrilateral Sort Map

Square	Rectangle
Rhombus	Trapezoid






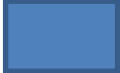




Quadrilateral Challenge

Quadrilateral Properties

4 square corners (right angles)	One pair of sides that go the same way (parallel)	Both pairs of opposite side are equal (congruent)	Both pairs of opposite side are equal (congruent)
4 square corners (right angles)	Both pairs of sides go the same way (parallel)	One pair of opposite sides do NOT go the same way (NOT parallel)	All 4 sides are equal (congruent)
4 corners but none are square (right angles)	Both pairs of sides go the same way (parallel)	Both pairs of sides go the same way (parallel)	All 4 sides are equal (congruent)
4 sides	4 sides	4 sides	4 sides
			
			

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 Common Core Georgia Performance Standards Framework
Third Grade Mathematics • Unit 5

4 square corners (right angles)	One pair of sides that go the same way (parallel)	Both pairs of opposite side are equal (congruent)	Both pairs of opposite side are equal (congruent)
4 square corners (right angles)	Both pairs of sides go the same way (parallel)	One pair of opposite sides do NOT go the same way (NOT parallel)	All 4 sides are equal (congruent)
4 corners but none are square (right angles)	Both pairs of sides go the same way (parallel)	Both pairs of sides go the same way (parallel)	All 4 sides are equal (congruent)
4 sides	4 sides	4 sides	4 sides
			
			

PRACTICE TASK: QUADRILATERAL RIDDLES

Adapted from Pennsylvania DOE activity Attributes of Two-Dimensional Shapes

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students have had some opportunities to look at quadrilaterals and begin to understand the categories that the shapes fit in based on the properties of the shapes. Additional time in studying the shapes may be needed based on the van Hiele levels of Geometric Thinking. Additional information about the levels may be found in the Van de Walle Resource book on pages 206-208

ESSENTIAL QUESTIONS

- How can we use two- dimensional shapes to solve problems?
- How do attributes help us describe shapes?
- Why is it important to know what quadrilaterals are and the differences between them?

MATERIALS

- Display the Riddle sheet using a document reader/ overhead projector or write the sentences on the board for students to copy.
- Varied of quadrilaterals for visuals

GROUPING

Independent or Partner Task

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

In this task, students will use the mathematical vocabulary developed through this unit to describe the attributes of quadrilaterals. Students will use 2 quadrilaterals to fill out the riddle. The riddle follows the pattern:

If I were a _____

_____, I would
have _____

_____. I would
have _____

_____. But I
would not have _____
_____ because
that would be _____

_____.

The first three blanks refer to one quadrilateral; the last two blanks refer to the other quadrilateral.

Example: If I were a square, I would have 4 sides. I would have 4 corners. But I would not have only one set of parallel lines (or lines that run in the same direction) because that would be a trapezoid.

Throughout this unit, students should begin to identify and describe the attributes of various quadrilaterals beyond the common characteristic. What makes a square a rectangle but a rectangle can't be a square?

FORMATIVE ASSESSMENT QUESTIONS/PROMPTS

- What part of the task was the hardest for you?
- How would you explain to your parents or guardians the difference between the quadrilaterals?
- Why should you know that different shapes can be in the same category?
- When would you use this information as an adult?

DIFFERENTIATION

Extension:

- Have students further investigate the difference between parallelograms and trapezoids. Then have them write a riddle based on their findings.

Intervention:

- Allow students to use other shapes with the quadrilaterals.

TECHNOLOGY CONNECTIONS

- <http://illuminations.nctm.org/LessonDetail.aspx?id=L350> – Complete lesson on rectangles and parallelograms
- <http://illuminations.nctm.org/LessonDetail.aspx?id=L813> – Shape Up Lesson from Illumination

Name _____ Date _____

Quadrilateral Riddle

Choose two quadrilaterals that are similar but have at least one difference. The first three lines of the riddle refer to one quadrilateral and its attributes. The last two lines of the riddle refer to the second quadrilateral and its attribute(s) that make it different from the first quadrilateral. Use specific math vocabulary to describe the attributes.

If I were a _____

I would have _____.

I would have _____.

But I would not have _____

Because that would be _____.

Optional: try another riddle using two new quadrilaterals.

If I were a _____

I would have _____.

I would have _____.

But I would not have _____

Because that would be _____.

PRACTICE TASK: WHAT DO YOU SEE?

Adapted from the lesson Shapely Lines from <http://nrich.maths.org/7009>

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
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4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students will continue to develop their understanding of shapes through this art activity. It will help you understand if students see all four sided figures as quadrilaterals, all five sided figures as pentagons, etc. This understanding from the students will show if they are developing understanding of geometric figures and progressing through the Van Hiele Levels of Geometric Thinking.

ESSENTIAL QUESTIONS

- What might a quadrilateral look like?
- How do you know if a shape is a _____

quadrilateral (square, rectangle, rhombus, trapezoid, parallelogram etc.)?
- Does a _____

_____ (include any shape) always look the same?
- What is the difference between a regular and irregular polygon?

MATERIALS

- Plain Paper
- Pencil
- Ruler

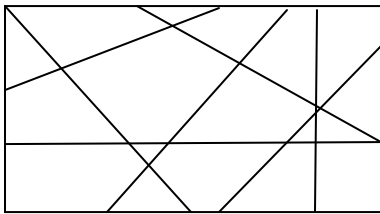
- Color Pencils
- Student Sheet

GROUPING

Individual Task

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

In this task, students will use a plain sheet of paper and a ruler to draw lines in all directions across the page. For example: their paper may look like this:



Students will then use colored pencils or crayons and color each type of shape a different color. For instance, I might want all my triangles to be green, all quadrilaterals purple, all pentagons red, etc. Some students may even want to separate their quadrilaterals and color all squares one color, rectangles a different color, etc. After coloring, students will then answer the questions on the student sheet about the different shapes they made from their lines. Some students will struggle to remember that a quadrilateral is any 4 sided figure, a pentagon is any 5 sided figure, a hexagon is any 6 sided figure.

FORMATIVE ASSESSMENT QUESTIONS

- Did you notice any patterns with your shapes?
- Did you have more of one shape than the others? Why do you think that?
- Did you have any irregular shaped polygons?

DIFFERENTIATION

Extension

- Students that had a good understanding of quadrilaterals may want to color or design each type of quadrilateral with a different color/design.

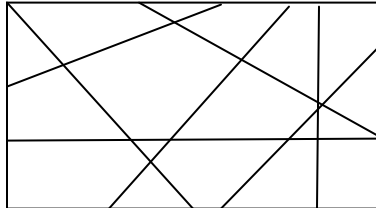
Intervention

- Students might need a demonstration of how to hold a ruler and draw a straight line. Others may need help holding the ruler as they draw straight lines. Students that are struggling to understand the differences in the types of shapes may need help to find all of the shapes that are alike.

Student Sheet

Name: _____ Date: _____

Directions: On a plain sheet of paper, use your pencil and a ruler to draw straight lines on your piece of paper to make an interesting pattern. You may use as many lines as you want but remember you will have to color each shape. Here is my example:



Now, use you color pencils or crayons to decorate each type of shape. For example, color or use some type of design to decorate all of your triangles the same. Change your color and/or design for all of your quadrilaterals. Continue until you have colored all of your shapes a unique color or design. Make sure to include a key to show what color you used for each shape.

Answer the following questions about your design.

1. Do you have any triangles? If so, how many? _____

2. Do you have any quadrilaterals? If so, how many? _____

3. Do you have any pentagons? If so, how many? _____

4. Do you have any hexagons? If so, how many? _____

5. Did you have any other shapes? If so, list them: _____

What do you see in your own pattern? _____

PRACTICE TASK: WHAT’S THE CONNECTION?

Adapted from the lesson, Quad Math from <http://rich.maths.org/6998/note>

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students have begun to learn more about quadrilaterals and their properties. In this task, students will use what they have learned about shapes to make a set of cards that are related to each other in a similar way.

ESSENTIAL QUESTIONS

- What are some things you have learned about quadrilaterals?
- How do you know the difference between a square, a rectangle, a trapezoid, and a rhombus?
- What might an irregular shaped quadrilateral look like?

MATERIALS

- A Rule card for every group of 4 players
- Page 1 and 2 for every group of 4 players
- Math Journal

GROUPING

Group of 4 – a 5th person could be in the group as a rule keeper or communicator for the group.

TASK DESCRIPTION

Students must follow the rules on the Rule Cards to play this game. They will help each other to form a group of 4 cards that relate to each other. To play, students will get into groups of 4. If there is a need, there can be a 5th person in each group who will act as the Rule Keeper or the communicator at the end. Distribute a rule card and the 16 cards to each group of players. Within the groups, distribute the 16 cards so that each player gets 4 cards. Place all cards face up and in front of each player where all players can see the cards. **REMEMBER**, the rules of the game include: no talking during the game, players can only give cards (not take), must have 2 cars in front of them at all times, and the team is successful when all 4 players have 4 cards that relate to each other. The goal of the game is that students will need to end up with a set of four cards in front of them that are related to each other in a similar way. The task is only successful if everyone on the team has completed their set.

For the teacher information only: the 16 cards consist of 4 squares, 4 rectangles, 4 trapezoids, and 4 irregular shaped quadrilaterals. Some groups may see a set consists of having 1 of each type of shape while others may see a set as having only one type of set. Either is correct **IF** students are able to explain their set.

When complete, have students write in their math journal their experience of the activity.

FORMATIVE ASSESSMENT QUESTIONS

- How are your cards related?
- What could have made this task easier?
- Is there another way to form a set with these cards?
- Did you all agree on the set to begin with or did you have to trade cards several times?
- What if a rhombus had been added to the deck of cards? Could you have still formed a set?

DIFFERENTIATION

Extension

- Create a similar game using more shapes, including rhombus and kite.

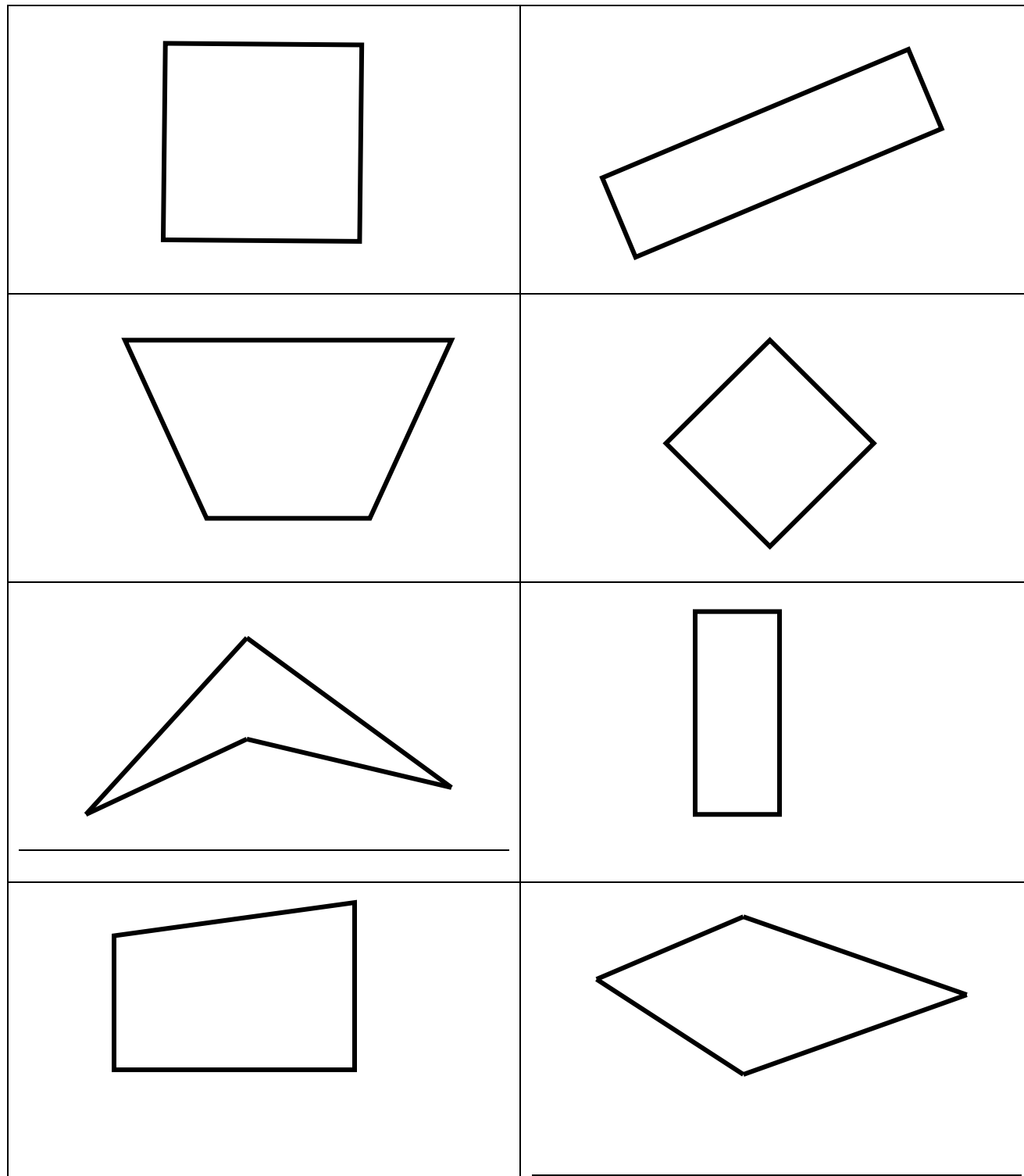
Intervention

- If student struggled to create sets that were related, have them talk about the cards and sort into groups based on their discussions. Make a chart to help the struggling student start to see the differences in the shapes.

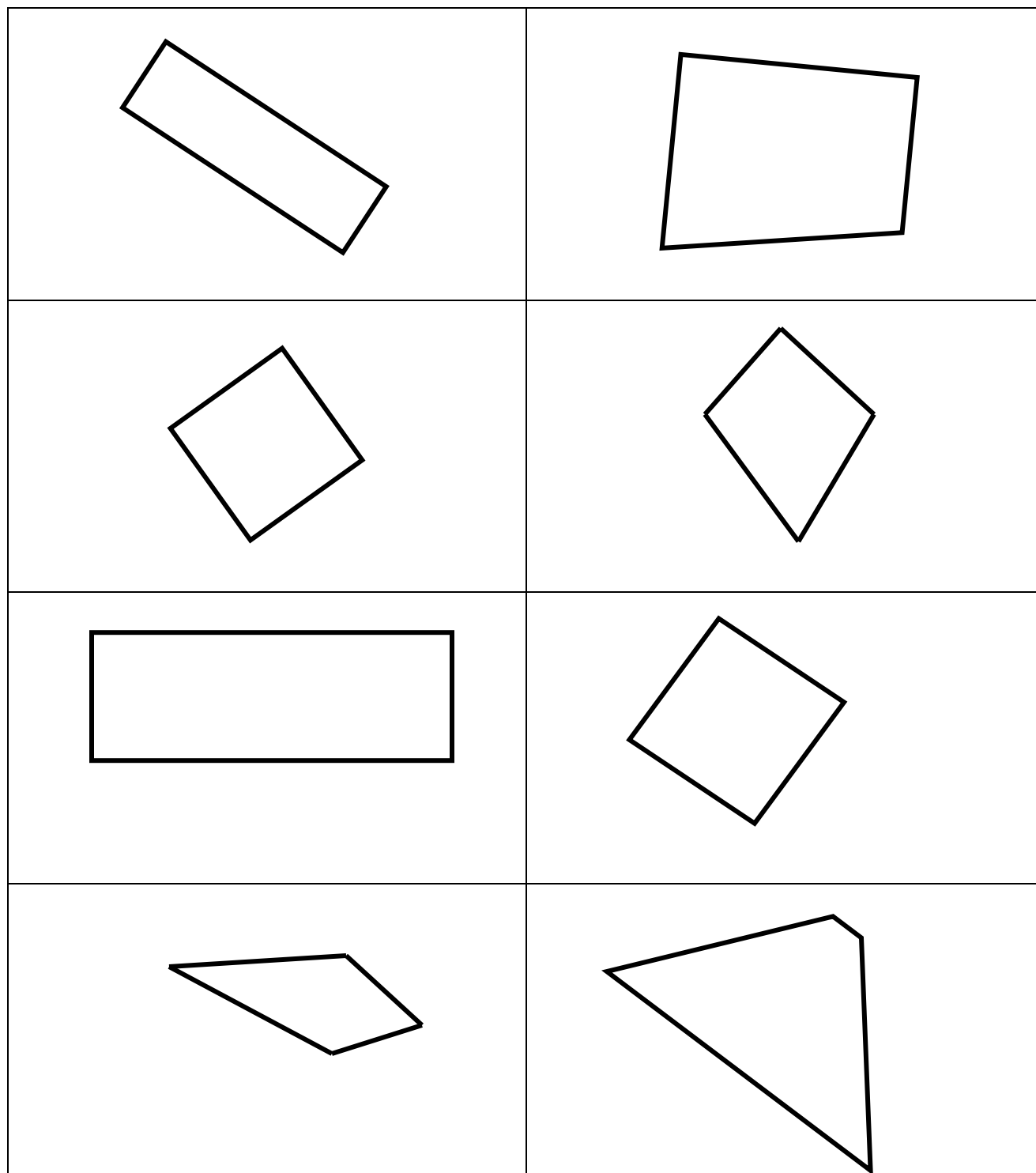
WHAT'S THE CONNECTION? Rule Cards

<p style="text-align: center;"><u>Rules</u></p> <p>You must not talk or use sign language. You can <u>give</u> cards to someone else. You must always have at least two cards in front of you. You <u>must not take</u> cards. You are only finished when everyone has a set of matching cards.</p>	<p style="text-align: center;"><u>Rules</u></p> <p>You must not talk or use sign language. You can <u>give</u> cards to someone else. You must always have at least two cards in front of you. You <u>must not take</u> cards. You are only finished when everyone has a set of matching cards.</p>
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WHAT'S THE CONNECTION? Playing Cards Page 1



WHAT'S THE CONNECTION? Playing Cards Page 2



CONSTRUCTING TASK: PATTERN BLOCK FRACTIONS

Adapted from the Lesson “Fun with Pattern Blocks” from NCTM’s Illuminations
<http://illuminations.nctm.org/LessonDetail.aspx?ID=L343>

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.2 Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.*

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Concepts about fractions are basic to mathematics but can pose challenges for students. In elementary schools, the most frequently used fraction models are the region and set models. This lesson exposes students to the region model and gives an opportunity for them to develop a thorough understanding of this model in multiple applications. As students work with a variety of fraction models in contexts that promote reasoning and problem solving, they develop a more thorough understanding of fractions and the relationships among them.

As the students work to understand fraction relationships using the region model, it is appropriate to work with concepts on a continuum from concrete to abstract. This lesson first exposes the students to a concrete representation of the region model through work with pattern blocks. As the students move toward more abstract work, it is appropriate to introduce semi-concrete representations. Having the students record fraction relationships pictorially gives them the opportunity to be exposed to such a model.

ESSENTIAL QUESTIONS

- Is there a way to represent the red trapezoid using blue and green pattern blocks?
- Can you cover the red trapezoid using only one color?
- What does this tell us about the relationship between the blue rhombus and the green triangle?
- Are there other ways to represent various pattern blocks (for example, the yellow hexagon) using more than one color pattern block?

- How do the relationships discovered with the pattern blocks help us understand fractions and area?
- What does $\frac{1}{3}$ look like in the hexagon? What does $\frac{1}{3}$ look like in the trapezoid? What does $\frac{1}{3}$ look like in the rhombus? Does one shape represent $\frac{1}{3}$ in all of the shapes?

MATERIALS

- Pattern Blocks (only hexagons, trapezoids, rhombuses and triangles are needed)
- Pattern Block Relationships Recording Sheet

GROUPING

Partner Task

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

For this lesson, the students need a set of pattern blocks. (Only the hexagons, trapezoids, rhombuses, and triangles are needed. The students do not use the square or the rhombus for this lesson.) If the students are seated at tables, one complete set of pattern blocks should serve an entire group.

The most common regions studied at the elementary grade levels are the rectangle and circle. The "region" represents the "whole," and parts of the region are all congruent. The students should be exposed to a variety of shapes and not limited to the rectangle and circle. It is important that the students work with a variety of regions so that they do not think of the region as only "pieces of a pie." For this reason, pattern blocks are an appropriate tool for work with the region model.

The students should use pattern blocks to answer the questions on the Pattern Block Relationship Sheet. Have the students record as many fraction relationships as possible. You may choose to have them record the relationships in a math journal to which they may refer later. Each pair should record relationships on chart paper to share with the whole class. As each pair shares, have the students add to their journal any relationships they may have missed.

As the students work to understand fraction relationships using the region model, it is appropriate to work with concepts on a continuum from concrete to abstract. This lesson first exposes the students to a concrete representation of the region model through work with pattern blocks. Having the students record fraction relationships pictorially gives them the opportunity to be exposed to such a model.

FORMATIVE ASSESSMENT QUESTIONS

It is important to know whether the students can do the following:

- understand that a fraction is part of a whole
- state the relationship between the pattern block shapes [e.g., that there are three triangles in one red trapezoid]
- identify fractions when the whole (region) and a part of the region are given
- represent the fractional relationship between the pattern block shapes using standard form of the written notation (e.g., the green triangle is x of the blue rhombus.)
- identify the numerator in a fraction and understand that the numerator is the top number in a fraction and indicates the number of parts of the whole
- identify the denominator in a fraction and understand that the denominator is the bottom number in a fraction and indicates the number of parts into which the whole is divided

The students' recordings can be used to make instructional decisions about their understanding of fraction relationships. Areas needing additional work can be developed during subsequent lessons. Fractions will be explored more in Unit 6.

- How many triangles does it take to make a hexagon?
- Show me more than one way to make a trapezoid. Write the fraction that each pattern block represents.
- Does $1/3$ represent the triangle in the rhombus and the hexagon? How do you know?

DIFFERENTIATION

Extension

If students understand the areas of the whole, some students might be ready to explore when the whole changes. Instead of representing the whole with one yellow hexagon, the students explore fractional relationships when two, three, and four yellow hexagons constitute the whole. See “Expanding our Pattern Block Repertoire” lesson from Illuminations <http://illuminations.nctm.org/LessonDetail.aspx?ID=L346>.

Intervention



- Most students should have used the fraction $1/2$ on numerous occasions. Lead the students in identifying and defining the numerator and denominator. Ask the students to explain what the top number in the fraction represents. [Students should indicate that this top number is the numerator and shows the number of parts of the whole.] The students should also identify the purpose of the bottom number, or denominator, as the number that indicates the number of parts into which the whole is divided. Since students are working in partners, all students should receive support from the peer or the teacher can guide the student through effective questioning.

TECHNOLOGY CONNECTIONS



- http://ejad.best.vwh.net/java/patterns/patterns_j.shtml - Pattern Blocks
- http://nlvm.usu.edu/en/nav/frames_asid_170_g_2_t_3.html?open=activities&from=category_g_2_t_3.html – National Library of Virtual Manipulatives

Pattern Block Relationships



NAME _____ Date _____

How many triangles  are in one rhombus  ? _____

What would be the fraction of 1 triangle in the rhombus? _____

How many triangles  are in one trapezoid  ? _____

What would be the fraction of 2 triangles in the trapezoid? _____

How many triangles  are in one hexagon  ? _____

What would be the fraction of 4 triangles in the hexagon? _____

How many rhombuses  are in one hexagon  ? _____

What would be the fraction of 3 rhombi in the hexagon? _____

How many trapezoids  are in one hexagon  ? _____

What would be the fraction of 1 trapezoid in the hexagon? _____

PRACTICE TASK: HOW MANY DIFFERENT WAYS CAN YOU FIND?

STANDARDS FOR MATHEMATICAL CONTENT:

MCC3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

MCC3.G.2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.*

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students should continue to develop their understanding of shapes by being given ample opportunities to explore with shapes and how they can be combined (composed) or (decomposed.)

ESSENTIAL QUESTIONS

- Is it possible to find more than 1 way for shapes to fit together to make another shape?
- What does it mean to partition a shape into parts?
- What do you know about pattern blocks that would help me understand how to fill an area?

MATERIALS

- How Many Ways Can You Find? Sheet
- Isometric Grid Paper (see the following pages or print from http://wps.ablongman.com/wps/media/objects/3464/3547873/blackline_masters/BLM_38.pdf) or Math Journal
- Pattern Blocks

GROUPING

Individual or Partner

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

In this task, students will discover different ways a plot of land can be divided to share equally among Uncle John’s nieces and nephews. Students have the option of dividing it between 2, 3, 4, 6, or 8 people. They may circle the number they are using for the task.

FORMATIVE ASSESSMENT QUESTIONS

- Have you shown all of the different ways you could divide the parcel of land? How do you know?
- How would we do this task with other shapes?
- Looking at your different solutions, how are they alike? How are they different?
- .Why did you decide to divide the land this way?

DIFFERENTIATION

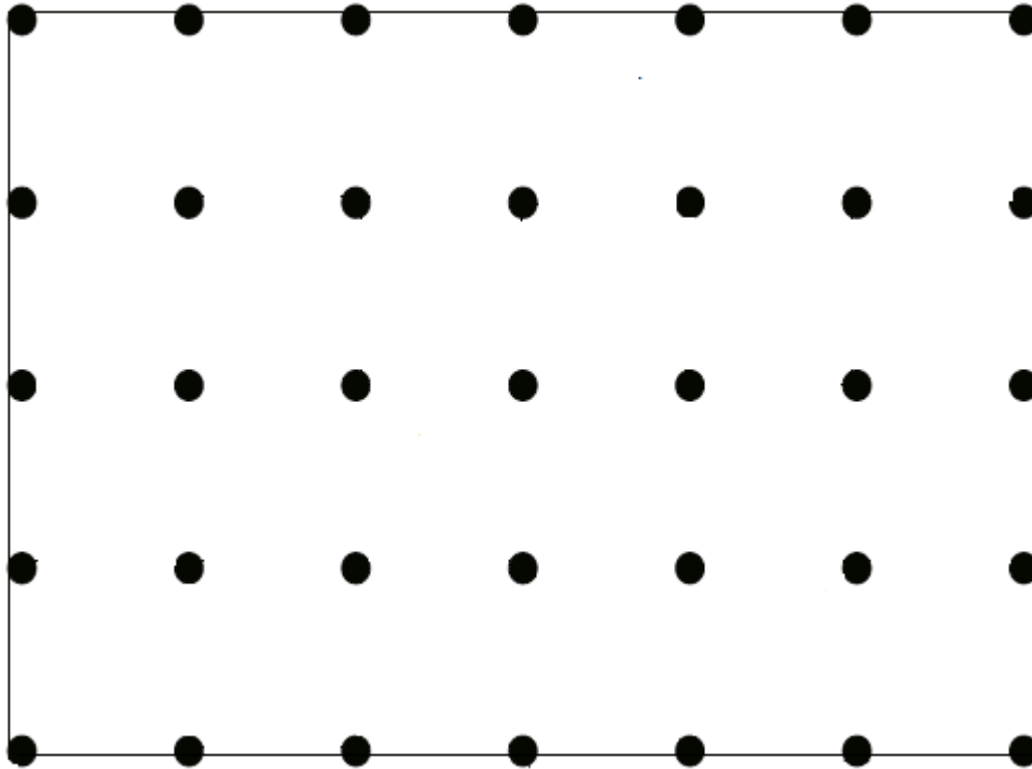
Extension

- Students can determine how to divide the parcel of land between five people.

Intervention

- Students may only divide the parcel of land between 4 students.

Great Uncle John has a parcel of land that measures 6 miles by 4 miles. In his will, he left the land to be divided equally among his (2, 3, 4, 6, or 8) nieces and nephews. However, he forgot to partition the land. Please help the nieces and nephews determine which parcel of land is theirs. Be sure to give everyone an equal amount of land. Use the blueprint below to help you.



How much land did Great Uncle John leave his nieces and nephews?

What does each person's share look like?

How do you know that each person's share is equal?

How did you determine the amount of land each person will get?

Is there another way that the land could have been divided?

PRACTICE TASK: PICTURE PIE

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.*

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students in 2nd grade will have started partitioning shapes (circles and rectangles) into equal areas of two, three, or four equal shares. In third grade, students will further develop this area by dividing shapes into halves, thirds, fourths, sixths and eighths. This activity gives students the opportunity to create pictures using fractional pieces of shapes.

In Picture Pie, Ed Emberley shows how a circle, which is divided into different fractional pieces, can be used to make pictures and patterns of all kinds.

In Picture Pie 2, Ed Emberley uses the included stencil to demonstrate how to draw a variety of things including pigs, wolves, clowns, bugs, and much more. You'll also find step-by-step instructions in both books. If these books are not available, you may use the shapes provided to create stencils, using file folders or stock paper, for students to trace around. You may shrink the pieces provided by using your copier machine to reduce each of the shapes if you wish to create smaller animals.

Clipart of circles and fractional pieces are obtained from
<http://etc.usf.edu/clipart/sitemap/fractions.php>

If rectangle or squares are needed, more polygons can be found at the same website.

ESSENTIAL QUESTIONS

- How can common shapes be used to create pictures?
- Is there a way to use parts of shapes to help create shapes?

MATERIALS

- Ed Emberley’s books Picture Pie: A Circle Drawing Book , Picture Pie 2: A Drawing Book and Stencil or similar books with pictures made from shapes, or Ed Emberley’s Website.
- Circles (see the following pages) or print smaller circle pieces from http://wps.ablongman.com/ab_vandewalle_math_6/0,12312,3547876-,00.html Blackline Masters 24, 25, 26

GROUPING

Individual or Group

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

To begin this task, either share Ed Emberley’s books (*Picture Pie* or *Picture Pie 2*) or visit his website:

<http://www.edemberley.com/pages/main.aspx?section=db&subSection=capPages>,

<http://www.edemberley.com/pages/main.aspx?section=db>.

Students will decide on a picture that they want to create. There is one circle included. Students should create fractional peices by folding the circle into halves, quarters, and eighths. This activity may take several days but can be used in a center or small group activity.

Once students finish their animals, they will create a chart to demonstrate their understandings of the fractional pieces. For example: In my animal, I used.... 6 $\frac{1}{2}$ circles, 5 $\frac{1}{4}$ circles, etc.

FORMATIVE ASSESSMENTS QUESTIONS

- What was difficult about this task?
- How many of each shape did you use?
- Did you have more $\frac{1}{2}$ or $\frac{1}{4}$ shapes?
- Did you discover a faster way of making your shapes?

DIFFERENTIATION

Extension

- Students should be allowed to create their own animals if desired.

Intervention

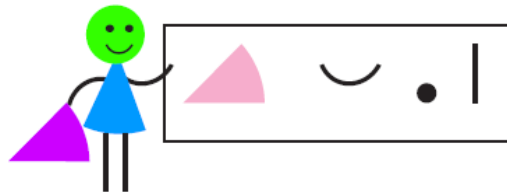
- Students that struggle with this activity will probably need to have an example in front of them. They may also need a demonstration on how to lay the stencil onto a piece of paper to trace around. If they need help to hold the stencil while tracing, consider allow a peer to help, tape the edges of the stencil in a few spots, or use a heavy object to hold the stencil in place.

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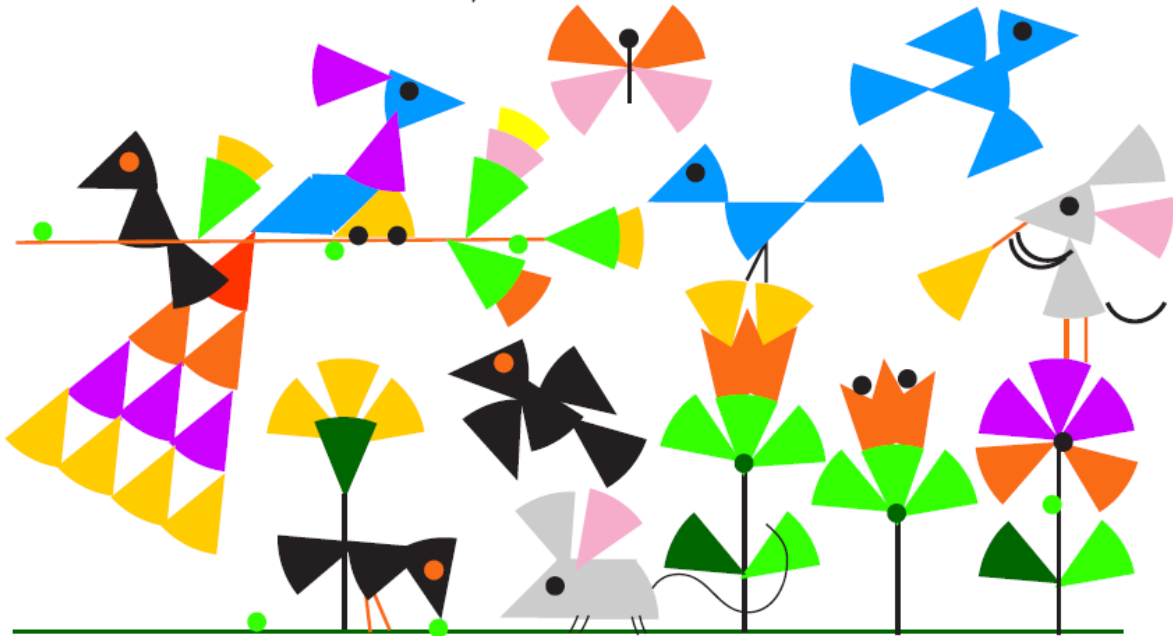
<http://www.edemberley.com/pages/main.aspx?section=legal>

Examples of Picture Pie Pictures

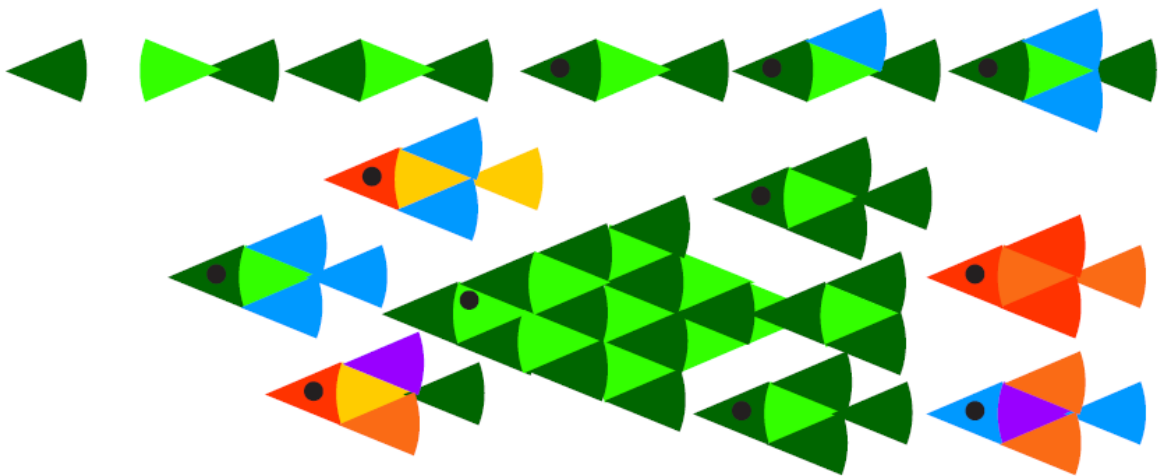
A lot, made with a little. I used this one Picture Pie Part.



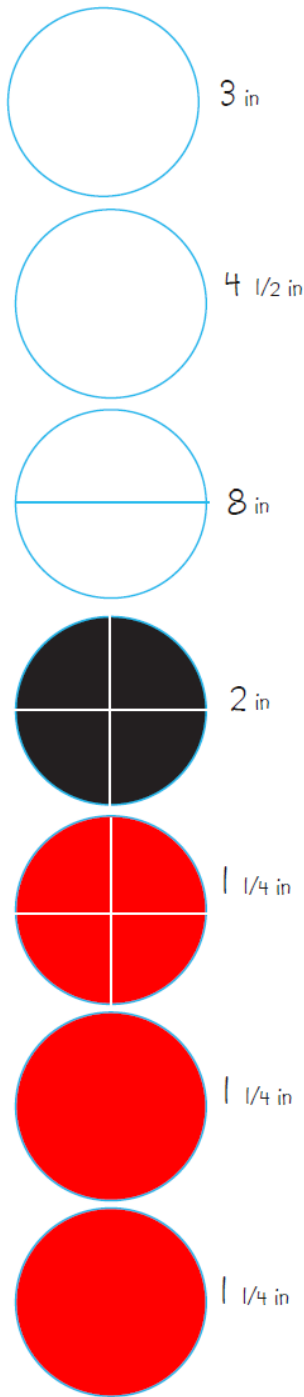
& a few dots and lines, to make these Picture Pie Pictures.



You can too. Step by step instructions show you how.

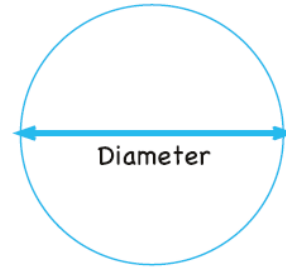


From www.edemberly.com



SCRATCH BUILT

To make this Picture Pie snowman from scratch you will need to make the following seven circles. Colors as shown. Diameter as shown. Divided as shown.



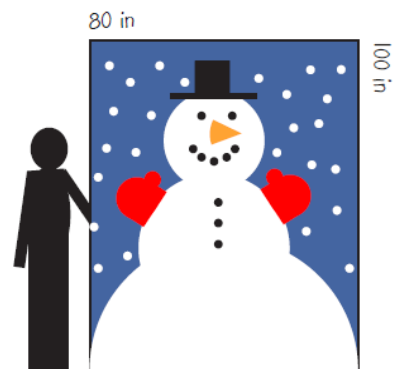
This snowman has been designed to fit on a standard sheet of construction paper, as shown.



For the 8X10 size only, You can save time, by using a standard office punch to make the mouth, eyes, and buttons.



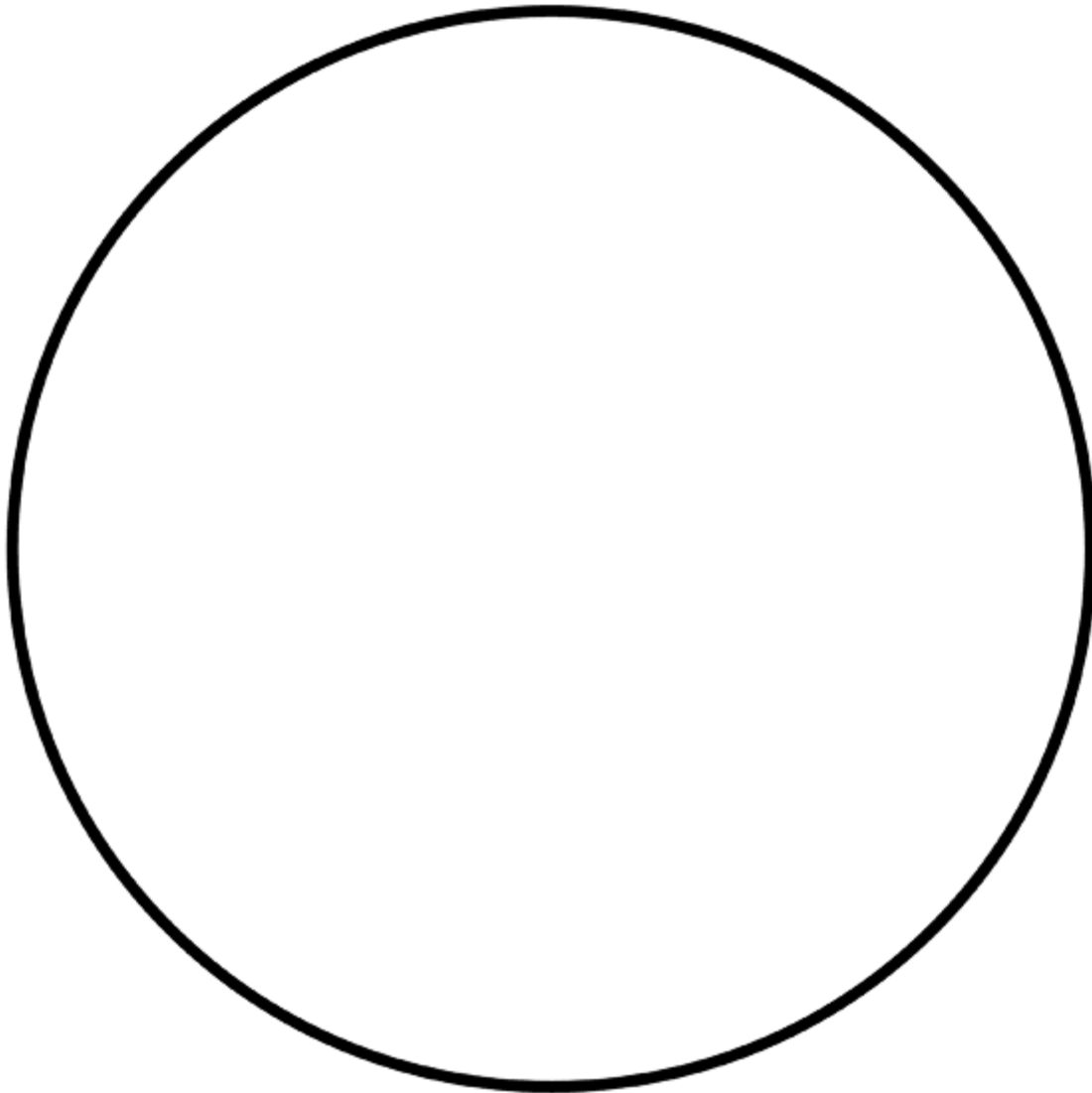
Double all measurements to make this same exact snowman fit a 16X20 inch background.



Multiply all measurements by 10, to make this same exact snowman fit an 80 X 100 inch background.

From Ed Emberley.com- Copyright© EdEmberley 2004

Fraction Pieces



One Whole

CONSTRUCTING TASK: PATTERN BLOCK GRAPHING

Images used from http://www.kellyskindergarten.com/math/math_activities.htm

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.MD.3 Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs. *For example, draw a bar graph in which each square in the bar graph might represent 5 pets.*

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND

Throughout each unit, students should continue to develop their understanding of collecting and representing data. In this task, students will use pattern blocks to create pictures and then collect data from their picture. Afterwards, they will represent this data in a picture and bar graph.

ESSENTIAL QUESTIONS

- In what ways can I represent data from a picture?
- How can I show what materials were used to create a picture?
- What type of intervals can be used in a picture or bar graph?

MATERIALS

- Pattern Block Pictures
- Isometric paper to represent their picture once created
http://www.ablongman.com/vandewalleseries/Vol_1_BLM_PDFs/BLM30-36.pdf (page 5)

GROUPING

Individual or Partner

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

Students will use the pattern block pictures to recreate a picture. You may use these examples or pattern block puzzles available from numerous resources including pattern books and the internet. This activity will help students to continue to develop their spatial sense. Students will not be able to use the picture to recreate the pattern block picture because it is not to scale. If you have students that need the pictures to scale, please visit http://www.kellyskindergarten.com/math/math_activities.htm to locate the pictures.

Once students create the pictures, they will use that information to create a scaled bar graph and picture graph to represent their data. Have students create questions that classmates can answer about their data. For example, how many more rhombi are used than triangles? Are there more hexagons or small rhombi used in my graph? Allow students time to analyze and interpret the data of their classmates.

FORMATIVE ASSESSMENT QUESTIONS

- Did you find it difficult to recreate the picture?
- Why did you decide to use ___ (2, 5, or 10) as the scale for your graphs? Was that your first choice? Was there a better number to use?
- Were classmates able to analyze and interpret your data?

DIFFERENTIATION

Extensions

- Students may want to create their own pictures with the pattern blocks.

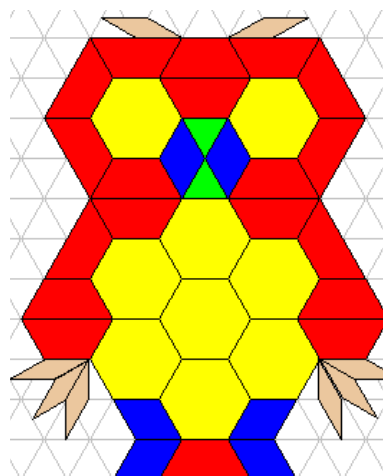
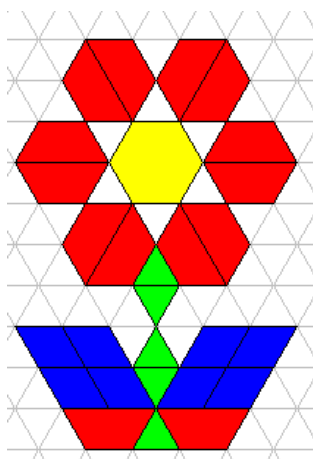
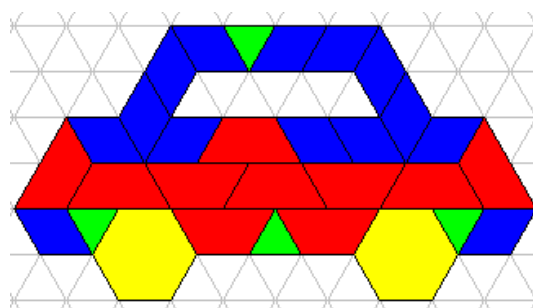
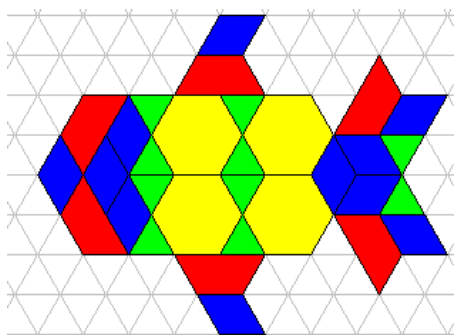
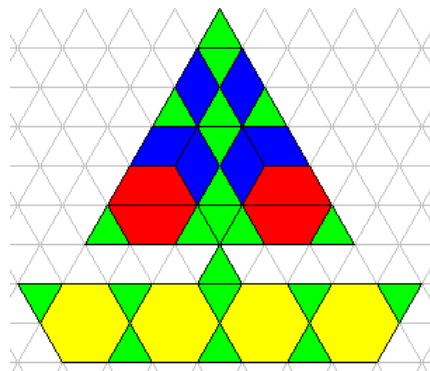
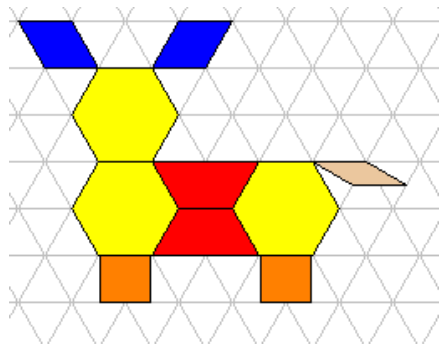
Interventions

- Students might struggle with this activity for several reasons. If a student struggles with recreating one of the pattern block pictures, print out the picture from http://www.kellyskindergarten.com/math/math_activities.htm. If the student struggles with assigning a scale, have students make a tally chart to show how many of each shape. Based on that information, a student can usually see a number that would be good to use. While five is a good benchmark, students should experience different intervals. For students that struggle, 2 is a better scale interval to show $\frac{1}{2}$ of a number.

TECHNOLOGY CONNECTIONS

- <http://nces.ed.gov/nceskids/createagraph/> - Create a bar graph online.
- http://www.softschools.com/math/data_analysis/pictograph/make_your_own_pictograph/
Create a Picture Graph

Samples of Pattern Block Pictures




Name _____

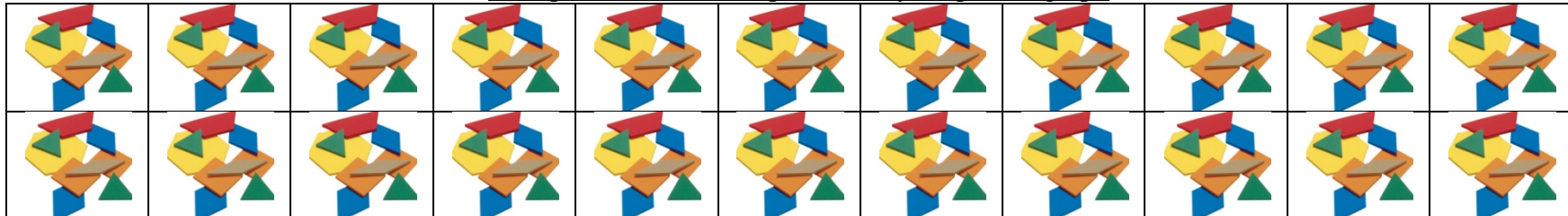
Date _____

Pattern Block Picture Data

Use your pattern block picture to fill in the picture graph. Remember to complete the key. Use a scale interval of 2, 5, or 10. Make sure you think about your scale before beginning to complete your graph.

<u>Title: _____</u>	
Hexagon	
Rhombus	
Trapezoid	
Square	
Small Rhombus	
Triangle	
Key  = _____ Pattern Blocks	

Cut apart and Use these pictures in your picture graph



PRACTICE TASK: I HAVE, WHO HAS?

Adapted from Mathwire.com's Game I have, Who Has?

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $\frac{1}{4}$ of the area of the shape.*

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.

BACKGROUND KNOWLEDGE

Students will have had experience dividing circles and rectangles into two, three, and four equal shares in third grade. This task will help students further develop their understanding of partitioning shapes into parts with equal area by using halves, thirds, fourths, sixths, and eighths.

ESSENTIAL QUESTIONS

- What is the purpose of studying fractions?
- How do you know if a shape shows _____ (halves, thirds, fourths, sixths, or eighths?)
- Describe what a fraction looks like in a shape?

MATERIALS

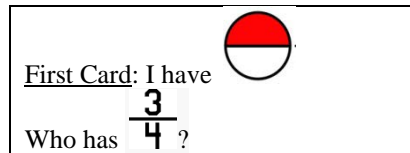
- I Have, Who Has Game Cards

GROUPING

- Whole Group

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

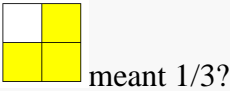
Print out and cut apart the three pages of I Have, Who Has? game cards. Randomly distribute **ALL** of the cards. There are 24 cards. Some students may have more than 1 card. If there are not enough cards, partner students up so that at least all partners get 1 card. Begin with the 1st card that says



Students will read the card aloud. Each player must pay attention to his/her card to know when it is their turn. Continue to play until the last card is read. The last card says that it is the last card. While the pictures are in color, the cards will print clearly if printed in gray scale.

FORMATIVE ASSESSMENT QUESTIONS

- How did you know what fraction you had?
- Why was it important to listen carefully?
- Is it possible to show each fraction in a different way? Show me your fraction in a different way.

- How could you help a friend who thought  meant $\frac{1}{3}$?




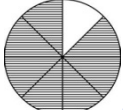



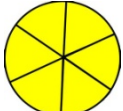

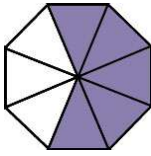
DIFFERENTIATION

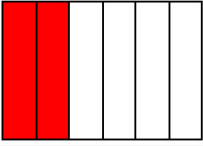
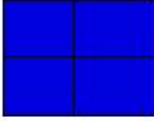

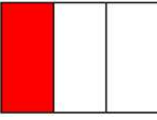

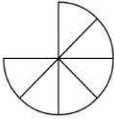
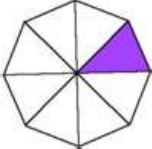

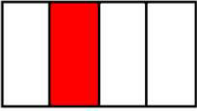

Extension

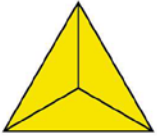
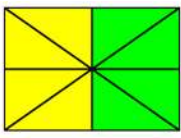

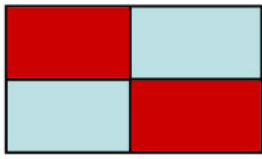
- Students may recreate the game with their own illustrations. They could also create a board game using fraction cards similar to these.

Intervention

- Students that struggle with fractions may need peer assistance during this game. Before beginning, give the student support by using questioning techniques to help them discover the fraction picture. They may need to write the fraction on the card or in their journal to help them remember the fraction as they play the game. It is possible to send a copy of this game home with the student to practice.

<p>First Card: I have </p> <p>Who has $\frac{3}{4}$?</p>	<p>I have </p> <p>Who has $\frac{4}{6}$?</p>
<p>I have </p> <p>Who has $\frac{7}{8}$?</p>	<p>I have </p> <p>Who has $\frac{2}{3}$?</p>
<p>I have </p> <p>Who has $\frac{2}{8}$?</p>	<p>I have </p> <p>Who has $\frac{3}{8}$?</p>
<p>I have </p> <p>Who has $\frac{6}{6}$?</p>	<p>I have </p> <p>Who has $\frac{1}{6}$?</p>
<p>I have </p> <p>Who has $\frac{5}{8}$?</p>	<p>I have </p> <p>Who has $\frac{2}{6}$?</p>

<p>I have </p> <p>Who has $\frac{4}{4}$?</p>	<p>I have </p> <p>Who has $\frac{1}{4}$?</p>
<p>I have </p> <p>Who has $\frac{1}{3}$?</p>	<p>I have </p> <p>Who has $\frac{5}{6}$?</p>
<p>I have </p> <p>Who has $\frac{6}{8}$?</p>	<p>I have </p> <p>Who has $\frac{1}{8}$?</p>
<p>I have </p> <p>Who has $\frac{2}{2}$?</p>	<p>I have </p> <p>Who has $\frac{1}{4}$?</p>
<p>I have </p> <p>Who has $\frac{8}{8}$?</p>	<p>I have </p> <p>Who has $\frac{3}{3}$?</p>

<p>I have </p> <p>Who has $\frac{4}{8}$?</p>	<p>I have </p> <p>Who has $\frac{3}{6}$?</p>
<p>I have </p> <p>Who has $\frac{2}{4}$?</p>	<p>I have </p> <p>Who has $\frac{1}{2}$?</p> <p>This is the last card.</p>

SCAFFOLDING/CONSTRUCTING TASK: MEASURING MY SHAPES

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.MD.4 Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units— whole numbers, halves, or quarters.

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students in second grade will have had some experience with rulers and measuring inch and $\frac{1}{2}$ inch. Later in 3rd grade, students will also learn to use the ruler to measure $\frac{1}{4}$ inch. In this activity, student will use rulers to measure each side of the shapes. After recording their information, students will make a line plot with the data collected.

ESSENTIAL QUESTIONS

- How do I use a ruler to measure length?
- How might I begin at any number on ruler to measure length?
- Explain how a line plot is made.

MATERIALS

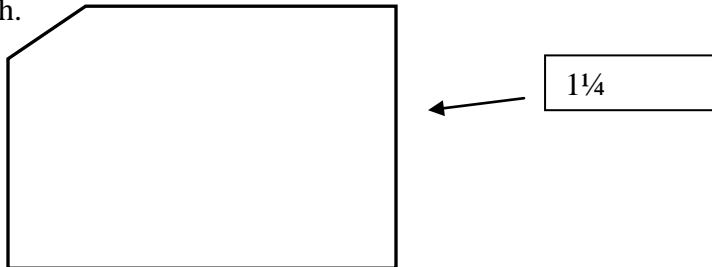
- Student Recording Sheet
- Rulers
- Plain Paper or Math Journal to make Line Plot

GROUPING

Partner or Individual

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

Students will use rulers to measure each side of the shapes on the Student Recording Sheet. All measurements are to the nearest inch or $\frac{1}{2}$ inch except for the pentagon shape below. The right side is $1\frac{1}{4}$ inch. This is good opportunity to preview Unit 7 with measuring to the nearest quarter inch.



There are 3 different types of rulers that can be printed from http://www.eduplace.com/math/mthexp/g3/visual/pdf/vs_g3_144.pdf. Print on stock paper and laminate to make sturdier.

After students record the measurements, you may wish to have them record the data in a chart. Students should also use the data to make a line plot, where the horizontal scale is marked off in appropriate units— whole numbers, halves, or quarters. At this point, students should be able to mark the whole numbers and halves as a review from second grade. You may wish to allow students to help construct a line plot together and add the quarter for the pentagon measurement. For more information about line plots, see the instructional strategies at the beginning of this unit or see page 333 in the Van de Walle resource book.

FORMATIVE ASSESSMENTS QUESTIONS

- How would you measure the shapes if you had a broken ruler?
- How would you explain to your parents/friends how you obtained your data?
- Explain why you made the line plot.

DIFFERENTIATION

Extension

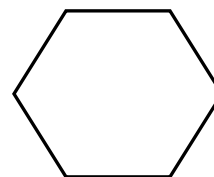
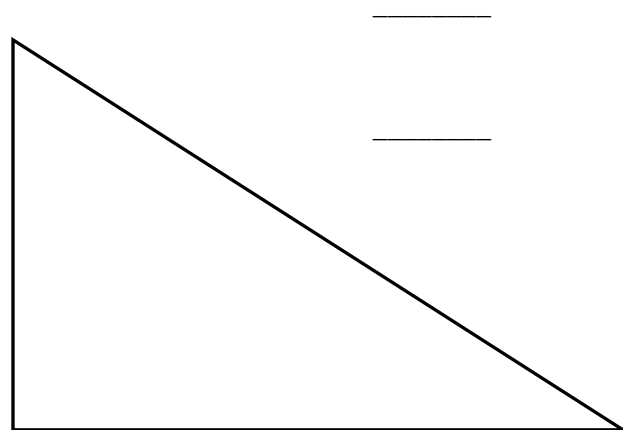
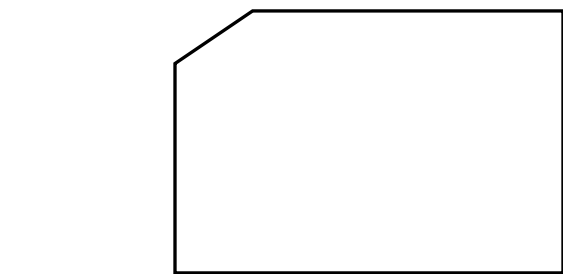
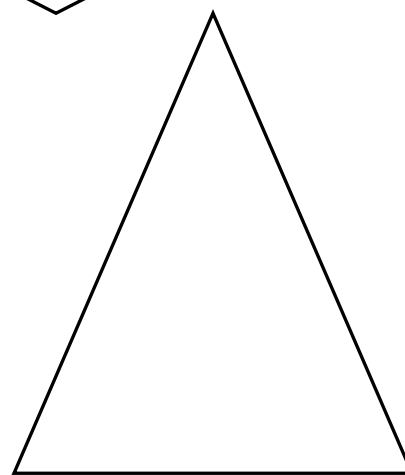
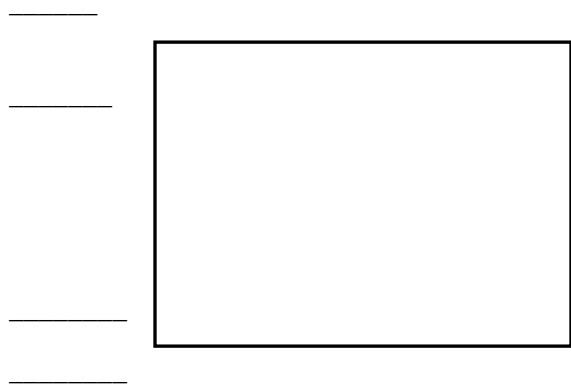
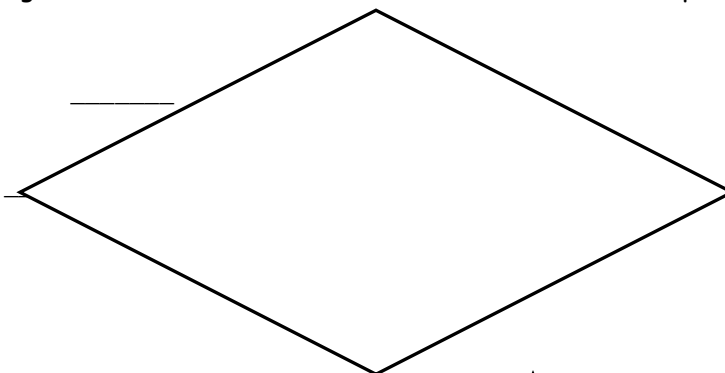
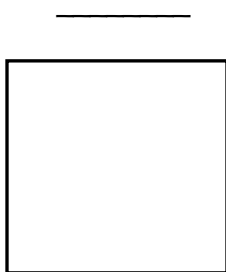
- You may want students to measure different shapes around the room, record the data, and make a line plot based on the shapes in your classroom.

Intervention

- Students who struggle may not be lining up the ruler correctly. They may also not know where halves are on a commercially produced ruler. You may want to print out the rulers provided above or use a paint marker/permanent marker to show halves on the ruler. Again, you can use this suggestion when you begin to teach quarters on the ruler.

Student Sheet

Directions: Using a ruler, measure each side of these shapes to the nearest inch, $\frac{1}{2}$ inch, or $\frac{1}{4}$ inch. Write your information on the lines along each side. Then, use the information to make a line plot.



CONSTRUCTING TASK: CREATING A GEOMETRY BOOK

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

MCC3.G.2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.*

STANDARDS FOR MATHEMATICAL PRACTICES

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

At this point, students should be able to describe shapes and sort the shapes according to their attributes. They should know quadrilaterals are polygons with four sides. Quadrilaterals include rectangles, rhombi, and squares. These shapes are a particular type of quadrilateral (parallelograms). Students should identify rhombus, rectangle, square, etc. as examples of quadrilaterals. They should also draw examples of quadrilaterals that do not belong to any subcategory (not rhombi, rectangles, or squares, etc.) such as trapezoids and/ or various sizes and shapes of convex and concave quadrilaterals.

ESSENTIAL QUESTIONS

- What are some differences between the quadrilaterals?
- How are the quadrilaterals alike?
- What is the difference between a trapezoid and a rhombus?

MATERIALS

- Plain Paper
- Crayons, Markers, Color Pencils

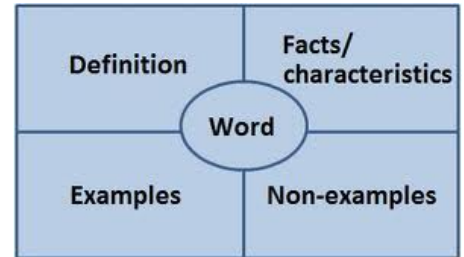
GROUPING

Individual or Partner

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

Students will use a vocabulary graphic organizer like the one to the right to make a booklet that demonstrates all that they have learned about the MCC3.G standard including shapes and partitioning shapes into equal areas.

Students could include the words: **triangles, quadrilaterals, pentagons, hexagons, trapezoid, square, rhombus, halves, thirds, fourths, sixths, eighths**. Allow students to make a chart of words that they have learned through this unit. They should be allowed to pick from this list. Share the rubric that is attached with students and then set a deadline for when they should have the project done.



FORMATIVE ASSESSMENT QUESTIONS/PROMPTS

- What did you learn from this unit?
- How will you remember it until next year?
- Which task did you like the most? The least?
- Is there a resource that you liked the most?
- Where can you find facts and characteristics of shapes?

DIFFERENTIATION

Extensions

- Allow for creativity including making models of the vocabulary words.

Interventions

- Students should consult their math journals or anchor charts that were created to help them complete this task. The Frayer model sheet is provided so that students that struggle do not have to recreate the graphic organizer but can focus on filling it in.

Georgia Department of Education
 Common Core Georgia Performance Standards Framework
Third Grade Mathematics • Unit 5

Rubric for Vocabulary Words

Name: _____

Date: _____

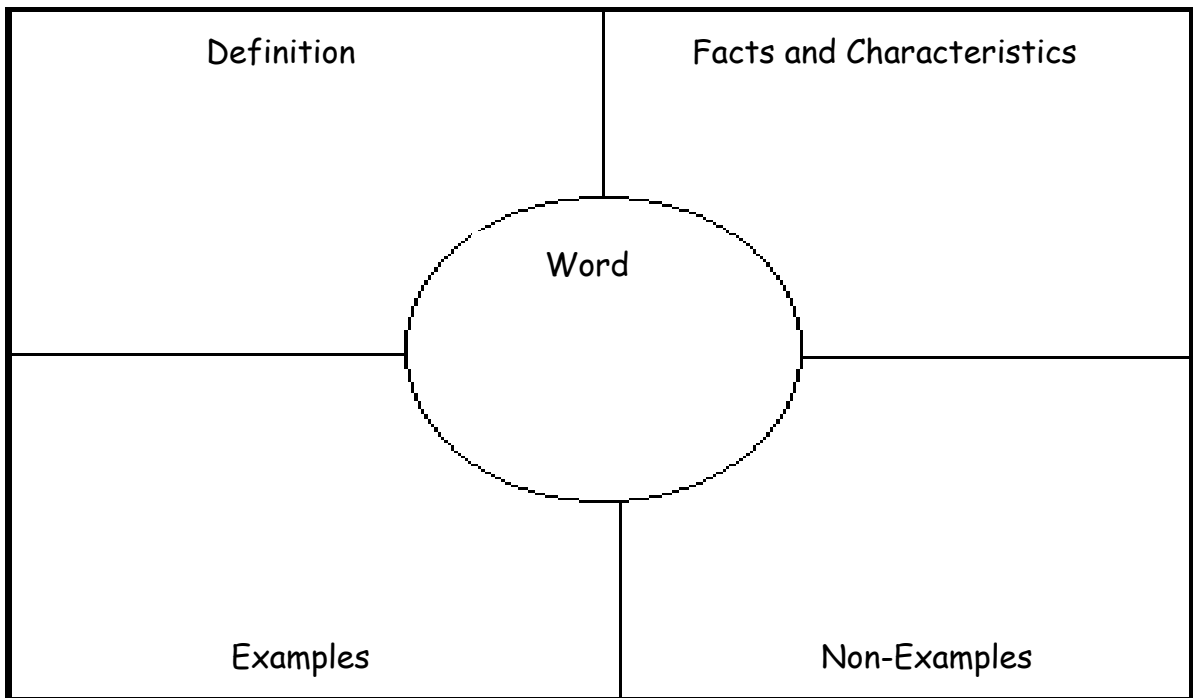
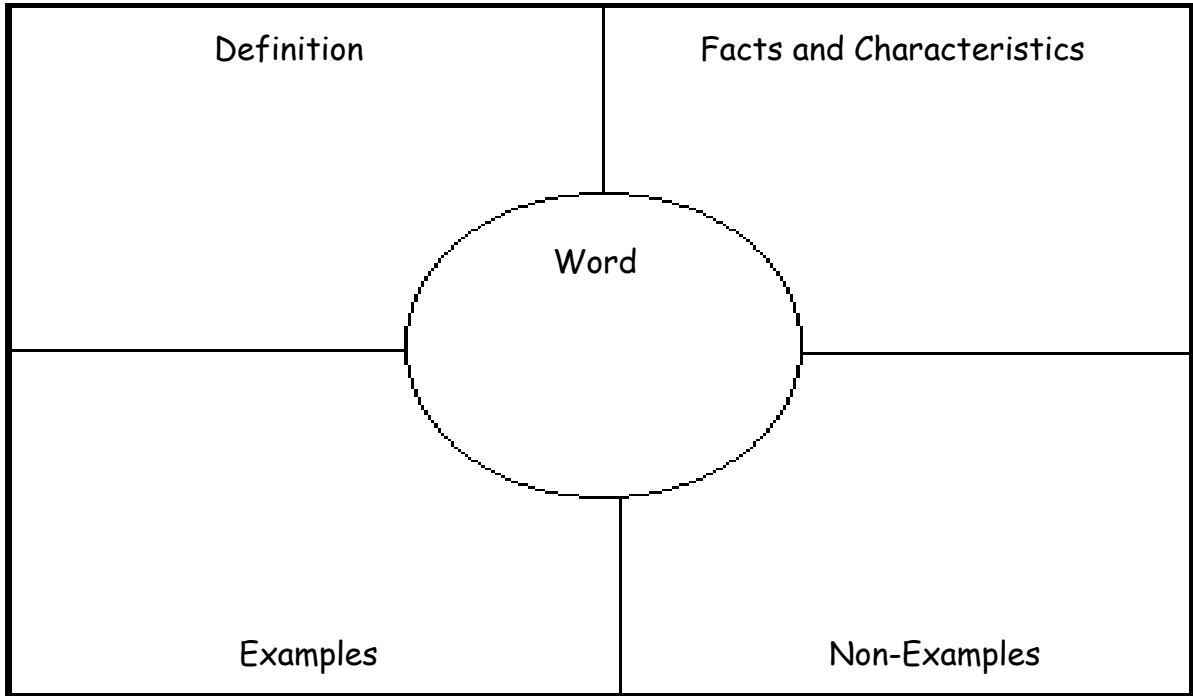
Indicator	3	2	1
Words Identified	Identified more than 5 words.	Identified 3 or 4 words.	Identified less than 3 words.
Definitions	Definitions were detailed and accurately matched the meaning of the word.	Definitions accurately matched the meaning of the word.	Most definitions accurately matched the meaning of the word.
Facts and Characteristics	Facts and Characteristics were detailed and accurately matched the meaning of the word.	Facts and Characteristics accurately matched the meaning of the word.	Most facts and characteristics accurately matched the meaning of the word.
Example and Non-examples	Example and Non-examples were detailed and accurately matched the meaning of the word.	Example and Non-examples accurately matched the meaning of the word.	Most accurately matched the meaning of the word.
Appearance	Responses were neatly written and easy to read.	Responses were fairly neatly written and readable.	Responses were not neatly written and difficult to read.

Rubric for Vocabulary Words

Name: _____

Date: _____

Indicator	3	2	1
Words Identified	Identified more than 5 words.	Identified 3 or 4 words.	Identified less than 3 words.
Definitions	Definitions were detailed and accurately matched the meaning of the word.	Definitions accurately matched the meaning of the word.	Most definitions accurately matched the meaning of the word.
Facts and Characteristics	Facts and Characteristics were detailed and accurately matched the meaning of the word.	Facts and Characteristics accurately matched the meaning of the word.	Most facts and characteristics accurately matched the meaning of the word.
Example and Non-examples	Example and Non-examples were detailed and accurately matched the meaning of the word.	Example and Non-examples accurately matched the meaning of the word.	Most accurately matched the meaning of the word.
Appearance	Responses were neatly written and easy to read.	Responses were fairly neatly written and readable.	Responses were not neatly written and difficult to read.



CULMINATING TASK: CHOICE BOARD

STANDARDS FOR MATHEMATICAL CONTENT

MCC3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

MCC3.G.2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.*

MCC3.MD. 3 Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs. *For example, draw a bar graph in which each square in the bar graph might represent 5 pets.*

MCC3.MD.4 Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units— whole numbers, halves, or quarters.

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Throughout this unit, students have reasoned with shapes and their attributes, including learning about quadrilaterals and partitioning all shapes into equal areas. Students have also had the chance to represent and interpret data through scaled picture and bar graphs. They should have also generated measurement data and displayed the data on a line plot. Since this is the performance task for the unit, students should be able to show what they know from this unit.

ESSENTIAL QUESTIONS

- What do you know about a quadrilateral that you didn't know at the beginning of this unit?
- How can you show what you have learned about quadrilaterals and other shapes?
- How would you explain to a younger student about the different shapes and how some shapes can share attributes?

- Can all shapes be split into halves, thirds, fourths, sixths and eighths? Prove it.

MATERIALS

- Choice Board Activity Sheet
- Rubric

GROUPING

Individual/ Group/Partner

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

Students will be given the Choice Board Activity sheet and the Rubric for the Choice Board Activity. Read each of the activities with the students and discuss the rubric that students will be scored with. In order to show master of the standards that are presented in this unit, students should complete at least one activity with each letter. Activity A will show standard MCC3.G.1. Activity B will show standard MCC3.G.2. Activity C will show standards MCC3.MD.3 and MCC3.MD.4 Allow students several days (make a deadline within your class) to create, finalize, and present their activity from the Choice Board Activity Sheet. Assist students during the creation stage.

FORMATIVE ASSESSMENT QUESTIONS

- How will you show your classmates what you have learned through this unit?
- Is there something that still confuses you about shapes, data, or measurement?
- Would you rather work with a partner for this task? How will you make sure you both are represented through the final project?

DIFFERENTIATION

Extension

- Students that need the extension may wish to do more than one or two of the activities. Students could be given time outside the classroom to work on additional activities.

Intervention

- Students may need assistance with many of the activities. Support these students by allowing them to work with a partner or providing additional support.

Geometry Choice Board

Student Directions: Show what you have learned from this unit. Pick one activity with an **A**, one activity with a **B**, and one activity with a **C** from the following activities to demonstrate to your classmates what you have learned.

<u>A</u>	<u>A</u>	<u>B</u>
Pretend you are square. Write a letter to another quadrilateral (rectangle, rhombus, or parallelogram) telling her/him why you should be a part of his/her class. List specific likenesses/differences.	Design a power point presentation on Quadrilaterals. Use at least five vocabulary terms in your power point that you have learned through this unit. Include the definitions and pictures.	Make a poster that shows shapes partitioned into equal areas of half, thirds, fourths, sixths, and eighths. Remember to show a variety of shapes and show the same shape partitioned in several ways.
<u>C</u>	<u>A/B</u>	<u>A</u>
Draw 5 shapes onto a piece of paper. Walk around your classroom or school for 10 minutes. Tally each shape that was seen. Create a bar graph or picture graph with this data. Remember to use a scale other than one to represent your data.	Design a bulletin board idea for our classroom. Show examples of posters, worksheets, or projects from this unit that should be shown. Be sure to include examples for MCC3.G.1 and MCC3.G.2. Turn in an example mini sheet of what the bulletin board would look like.	Find a website or game online that gives information about quadrilaterals. Give a small presentation explaining what you can learn about quadrilaterals from the website.
<u>A/B</u>	<u>C</u>	<u>C</u>
Create a game for all of the shapes learned. Also include partitioning of the shapes in the game. Think of the cards needed, pieces and game board you want to use. Attach written instructions for how to play.	Find 15 items around the room and measure them to the nearest inch or $\frac{1}{2}$ inch. Make a table and create a line plot showing your data.	Survey your class and another class about their favorite shape. Display the information using a bar graph and a picture graph. Remember to use a scale other than one to represent the data.

Rubric for Choice Board Activity

CATEGORY	Outstanding	Good	Fair	Poor
Content	Presentation content is engaging and interesting and appropriate for the intended audience.	Presentation content contains interesting information, but has limited appropriateness for the audience.	Presentation content has relevance, but is not appropriate for the audience.	Content is not relevant and does not focus on learning assessment.
Preparation	The presenter is well prepared with all necessary materials. Includes more than one activity for A, B, and C.	Most of the necessary materials are readily available. Includes at least one activity for A, B, and C.	Some of the necessary materials are unavailable or cannot be located. Includes only 2 activities.	The presenter displays a lack of preparation and lacks necessary materials. Only includes 1 activity for A, B or C.
Presentation	Presentation is engaging and easily understood and clearly stated for the audience.	Presentation is understood, but offers limited engagement of the audience.	Presentation has value, but is not engaging for the audience.	Presentation is not engaging and does not offer worthwhile information for the audience.
Relevance	Presentation demonstrates a clear connection to the student and his/her success in math.	Presentation is relevant, but no support is given for "why" the assessment is relevant to success in math.	Presentation has little relevance to the child's success in math.	Presentation is not relevant to the child's success in math.
Impact	This presentation will have a significant impact on my students' success in math.	This presentation will have a positive impact on my students' success in math.	This presentation will have a minor impact on my students' success in math.	This presentation will have no impact on my students' success in math.